

Algorithmic Aspects of Throughput-Delay Performance for Fast Data Collection in Sensor Networks

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Thesis Statement:

Multi-channel **scheduling**, optimal **routing** topologies, and **transmission power control** are necessary in order to improve the **throughput-delay** trade-off for **aggregated convergecast** in large-scale, multi-hop, wireless sensor networks.

Outline

1 Maximizing Convergecast Throughput

- Motivation and Preliminaries
- Scheduling with Unlimited Frequencies
- Approximations on Unit Disk Graphs
- Approximations on General Disk Graphs

2 Multi-Channel Scheduling in SINR

- Motivation and Interference Models
- Problem Formulation and Approach
- Approximations in SINR

3 Throughput-Delay Trade-off

- Motivation
- Bi-criteria Formulation
- Optimal Spanning Trees (parts)

4 Distributed Topology Control in 3-D

- Motivation
- Two Approaches: Orthographic Projections, SDT

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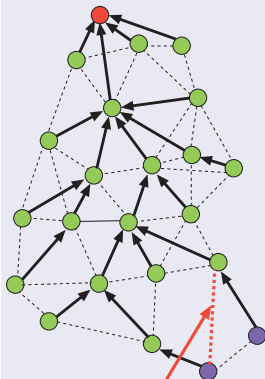
- Motivation and Interference Models
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4 Conclusions

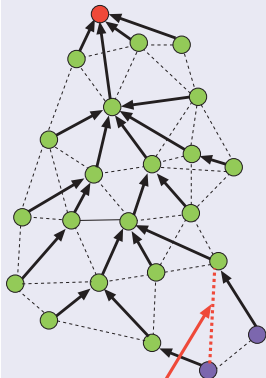
Model and Assumptions



Secondary conflict

e.g., Applications with fast & efficient data collection requirements.

Model and Assumptions



Secondary conflict

e.g., Applications with fast & efficient data collection requirements.

- TDMA **periodic** scheduling
 (- every node generates a **single packet** at the beginning of each frame
 - every node transmits once per slot)
- **Graph-based** network & interference model
- **Half-duplex**, single transceiver
- **Receiver-based Frequency Assignment**
- **Non-interfering** orthogonal channels
- In-network **aggregation**
 (**distributive**, **algebraic**)
 - aggregation happens at each hop)



Schedule length

Convergecast and Benefits of Multiple Frequencies

Convergecast

A **many-to-one** communication pattern (i.e., flow of data): from all the nodes to a sink (opposite of broadcast).

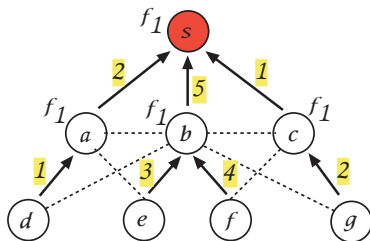


Figure: Schedule length is 5.

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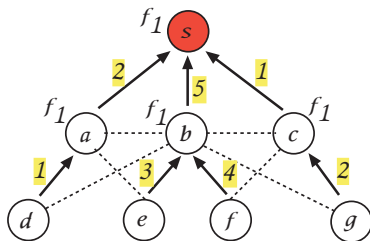


Figure: Schedule length is 5.

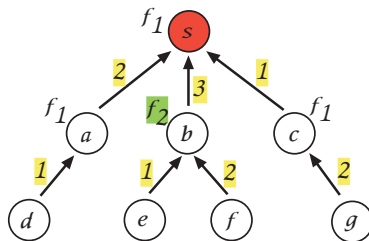


Figure: Schedule length is 3.

Convergecast and Benefits of Multiple Frequencies

Convergecast

A **many-to-one** communication pattern (i.e., flow of data): from all the nodes to a sink (opposite of broadcast).

	Frame 1			Frame 2		
Receiver	Slot 1	Slot 2	Slot 3	Slot 1	Slot 2	Slot 3
<i>s</i>	<i>c</i>	<i>a d</i>	<i>b e f</i>	<i>c g</i>	<i>a d</i>	<i>b e f</i>
<i>a</i>	<i>d</i>			<i>d</i>		
<i>b</i>	<i>e</i>	<i>f</i>		<i>e</i>	<i>f</i>	
<i>c</i>		<i>g</i>			<i>g</i>	

Pipelining

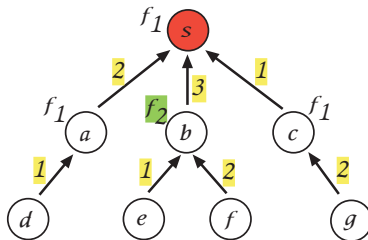


Figure: Schedule length is 3.

Problem Formulation

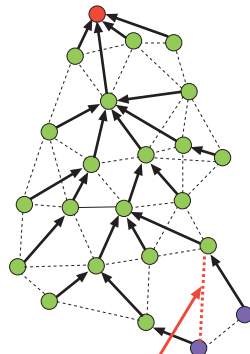
Joint Frequency and Time Slot Assignment

Given a connected network $G = (V, E)$ of arbitrarily deployed nodes, K orthogonal frequencies, and a routing tree $T \subseteq G$ rooted at the sink $s \in V$

- Assign a frequency to each **receiver** in T
- Assign a time slot to each **edge** in T

such that the **aggregated throughput** at the sink is **maximized**, where

Aggregated Throughput = $1/\text{Schedule Length}$
(equivalent to minimizing the Schedule Length)



Secondary conflict

Scheduling Complexity

Theorem

Joint Frequency and Time Slot Assignment is NP-hard on general graphs.

Proof: Reduction from **Vertex Color**.

Questions

- Does the problem still remain NP-hard with **unlimited** frequencies?
- If not, how many frequencies (at a min, or at most) are needed?
- Can we design algorithms that have **provable, worst-case** guarantee?

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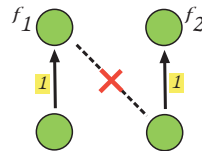
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Theorem

Given a spanning tree T on a graph $G = (V, E)$, finding the **minimum** number of frequencies required to remove **all** secondary conflicts is NP-hard.

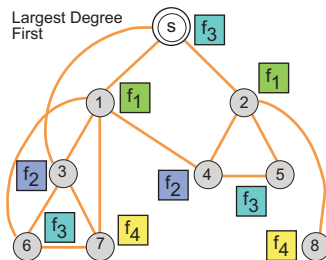
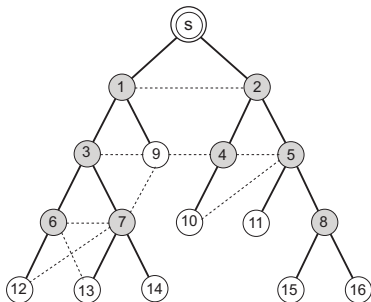


Secondary conflict

A Frequency Upper Bound

Constraint Graph

- For each receiver in G create a node in G_C .
- Create an edge between two nodes in G_C if the corresponding receivers in G form a secondary conflict.



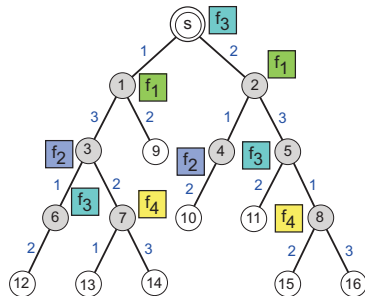
Lemma

$K_{max} \leq \Delta(G_C) + 1$, where $\Delta(G_C)$: max degree in G_C . (Vertex Color)

Time Slot Assignment

Algorithm: BFS-TIMEslotASSIGNMENT

1. **while** $E_T \neq \emptyset$ **do**
2. $e \leftarrow$ next edge from E_T in **BFS** order
3. Assign minimum time slot to e respecting adjacency constraint
4. $E_T \leftarrow E_T \setminus \{e\}$
5. **end while**



Theorem

BFS-TIMEslotASSIGNMENT gives a schedule of minimum length $\Delta(T)$, where $\Delta(T)$: maximum node degree in T .

Evaluation

Parameters:

- Number of nodes: $n : 200$, square region of area $A : 200 \times 200$
- Shortest Path Tree, Unit Disk Graph

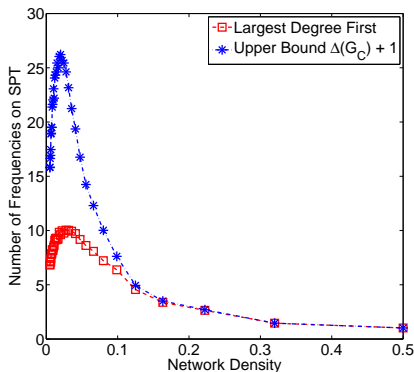


Figure: Number of frequencies required to remove all secondary conflicts as a function of network density n/A on SPT.

So far...

Joint Frequency and Time Slot Assignment is

- **NP-hard** with **limited** (constant number) frequencies on arbitrary graphs.
- **Polynomial** with **unlimited** (at most $\Delta(G_C) + 1$) frequencies for arbitrary graphs.

Next...

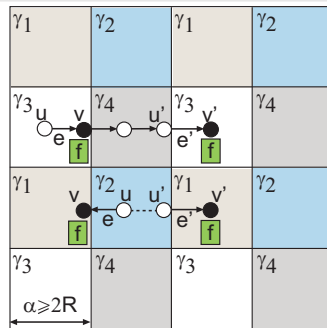
Approximation algorithms for **Random Geometric Graphs** with **limited** (constant number) frequencies.

- Uniform transmission range (**Unit Disk Graphs**)
- Non-uniform transmission range (**General Disk Graphs**)

Approximation on UDG

Algorithm \mathcal{A}_{UDG} Overview

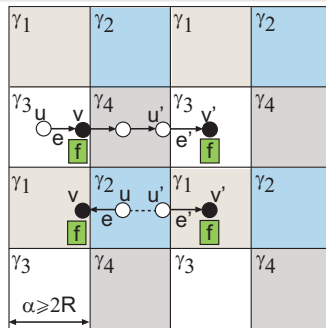
- **Phase 1:** Assign frequencies to the receivers in each cell such that the **maximum** number of nodes transmitting on the same frequency (**load**) is minimized. (**Load-Balanced Frequency Assignment**)
- **Phase 2:** Assign time slot greedily to each edge.



Approximation on UDG

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Theorem

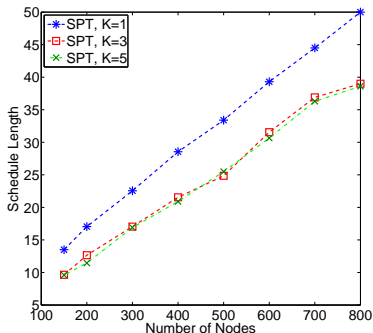
Algorithm \mathcal{A}_{UDG} achieves a **constant factor** $8\mu_\alpha \cdot \left(\frac{4}{3} - \frac{1}{3K}\right)$ approximation on the optimal schedule length, where $\mu_\alpha > 0$ is a constant for any given cell size $\alpha \geq 2R$, and given node deployment, where μ_α : maximum number of edges on the same frequency in any cell that can be scheduled simultaneously by any algorithm.

Evaluation

Parameters

UDG on a region of size 200×200 with transmission radius $R = 25$

Shortest Path Tree



Observations

- Schedule length decreases with increasing number of frequencies
- However, with diminishing returns
- Structure of the routing tree (high node degree) may lead to bottlenecks

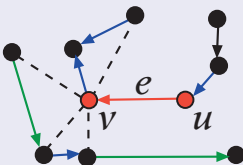
Approximation on Disk Graphs

Approximation on Disk Graphs

Notations

- $r(u)$: Transmission range of node u
- $\ell(e)$: Length of edge e
- $I(e)$: Set of edges that are either adjacent to e or form a secondary conflict with e
- $I_{\geq}(e)$: Subset of $I(e)$ that have larger disks than e

$$I_{\geq}(e) = \{e' = (u', v') : e' \in I(e), \ell(e') \geq \ell(e)\}$$



Approximation on Disk Graphs

Algorithm \mathcal{A}_{DG} Overview

- **Phase 1:** Assign frequencies such that the maximum number of edges interfering with any given edge is minimized.
 - **0 – 1 Integer Linear Program:** Define indicator variables X_{vk} for edge $e = (u, v)$ as:

$$X_{vk} = \begin{cases} 1, & \text{if receiver } v \text{ is assigned frequency } f_k \\ 0, & \text{otherwise} \end{cases}$$

A frequency assignment is a 0 – 1 assignment to $X_{vk}, \forall e, \forall f_k$.

Approximation on Disk Graphs

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- **Phase 2:** Sort edges in **non-increasing** order of **lengths**, and assign smallest available slots starting from the largest.

Approximation on Disk Graphs

0-1 Integer Linear Program of Frequency Assignment

Minimize λ

subject to :

$$\forall e = (u, v), \forall f_k : \sum_{v'} n(e, v') X_{vk} \leq \lambda \quad (1)$$

$$\forall e = (u, v) : \sum_{f_k} X_{vk} = 1, \quad (2)$$

$$\forall e = (u, v), \forall f_k : X_{vk} \in \{0, 1\} \quad (3)$$

- Solve the Linear Relaxation (LP) by modifying constraint (3)
- **Randomized Rounding:** Assign $Y_{vk} = 1$ with probability X_{vk}^* , where X_{vk}^* are the optimal fractional LP solutions, and Y_{vk} are the new integral random variables.

Approximation on Disk Graphs

Lemma

Let Y_{vk} be the rounded solution, as described above. Then,

$$\max_{e, f_k} \left\{ \sum_{e'=(u', v') \in I_{\geq}(e)} Y_{v'k} \right\} = O(\Delta(T) \log n \cdot \lambda^*),$$

with probability at least $(1 - 1/n)$.

Proof: Apply **Chernoff bound**.

Approximation on Disk Graphs

Lemma

Let $Y_{v'k}$ be the rounded solution, as described above. Then,

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Proof: Apply **Chernoff bound**.

Theorem

The schedule constructed by time slot assignment strategy along with the frequency assignment using the above randomized rounding procedure results in a schedule of length $O(\Delta(T) \cdot \log n)$ times the optimum.

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Realistic Interference Model

Limitations of a Graph-Based Model (Protocol Model)

- Interference is **binary** and stops abruptly beyond a distance - idealizes physical laws
- Fails to capture **cumulative interference** from (many) far-away transmitters
- Sometimes **pessimistic** decisions and **conflicting** schedules

Realistic Interference Model

SINR Model (Physical Model)

For a given frequency f , the received signal power from sender s_i to its intended receiver r_i is:

$$P_{r_i}(s_i) = \frac{P}{d(s_i, r_i)^\alpha},$$

where $\alpha \in [2, 6]$ is called the **path-loss exponent**; value depends on external conditions.

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A transmission from sender s_i to its intended receiver r_i is successful if the ratio, $SINR_{r_i}$, of the received signal power to the **cumulative interference** plus noise \mathcal{N} at r_i is more than a hardware-dependent threshold β :

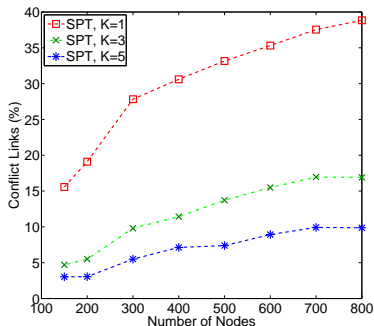
$$\begin{aligned} SINR_{r_i} = \frac{\frac{P}{d(s_i, r_i)^\alpha}}{I_{r_i} + \mathcal{N}} &= \frac{\frac{P}{d(s_i, r_i)^\alpha}}{\sum_{j \neq i} \frac{P}{d(s_j, r_i)^\alpha} + \mathcal{N}} \\ &\geq \beta \end{aligned}$$

Realistic Interference Model

Parameters

- CC2420 radio parameters with receiver sensitivity -95 dB
- Path-loss exponent $\alpha = 3.5$, transmit power -6 dB

Percentage of Conflicting Schedules: SINR vs. Graph-based Model



Observations

- For a given frequency, the amount of conflict increases as the network gets denser, reaching almost 40% for densest deployment with a single frequency
- With multiple frequencies, the amount of conflict is much less

Problem Formulation in SINR

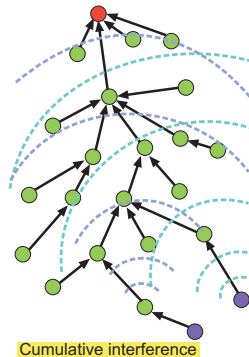
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Given a connected network of arbitrarily deployed nodes, K orthogonal frequencies, and a routing tree $T = (V, E_T)$ rooted at the sink $s \in V$

- Assign a frequency to each **receiver** in T
- Assign a time slot to each **edge** in T

such that the **schedule length** is **minimized**, subject to

$$\text{SINR}_{r_i} \geq \beta \text{ at every receiver } r_i$$



Approach

Link Diversity

Classify the edges in E_T based on their lengths $\ell_i = d(s_i, r_i)$. **Link diversity** is the number of magnitude of different lengths

$$g(E_T) = |\{m \mid \exists e_i, e_j \in E_T : \lfloor \log(\ell_i/\ell_j) \rfloor = m\}|$$

Usually a small constant in practice, but theoretically can be equal to the number of nodes

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Overall Idea

- **Normalize** (w.l.o.g) the minimum edge length to one
- Let

$$E = \{E_0, \dots, E_{\log(e_{max})}\}$$

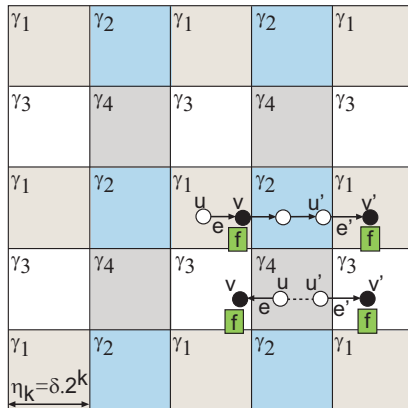
denote the set of non-empty length classes, where E_k is the set of edges of lengths in $[2^k, 2^{k+1})$, and e_{max} is the longest edge

- **Partition** the problem into **disjoint length classes**, and process edges in each class separately

Approach

For Length Class E_k

- Divide the 2-D region into a set C_k of square grids of length $\eta_k = \delta \cdot 2^k$, for some constant δ (will choose δ later)
- **Frequency Assignment:**
 - For each cell in C_k , run **FREQUENCYGREEDY** on the receivers
- **Time Slot Assignment:**
 - Four color the cells in C_k
 - Can we still reuse time slots across non-adjacent cells of the same color? If so, how many?



Approximation Algorithm in SINR

Theorem

For cells of the **same color** in C_k , we can simultaneously schedule **at most one** edge in E_k from every **non-adjacent** cell that lies on the **same frequency**, so long as the cell size satisfies:

$$\eta_k = \delta \cdot 2^k, \quad \text{for } \delta = 4 \left[8\beta \cdot \frac{\alpha - 1}{\alpha - 2} \right]^{\frac{1}{\alpha}},$$

where $\beta \geq 1$ is the SINR threshold, and $\alpha > 2$ is the path-loss exponent.

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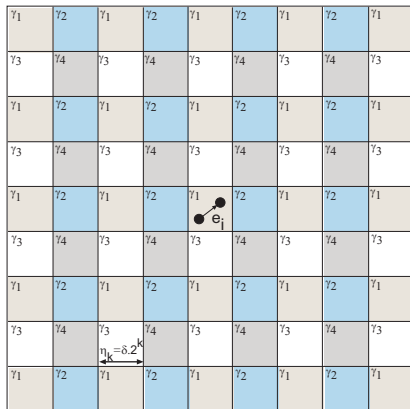
Proof Sketch

- Consider one specific edge $e_i = (s_i, r_i) \in E_k$ in any cell $c \in C_k$
- Received power at r_i

$$P_{r_i}(s_i) = \frac{P}{\ell_i^\alpha} \geq \frac{P}{2^{\alpha(k+1)}}, \quad \because 2^k \leq \ell_i < 2^{k+1}$$

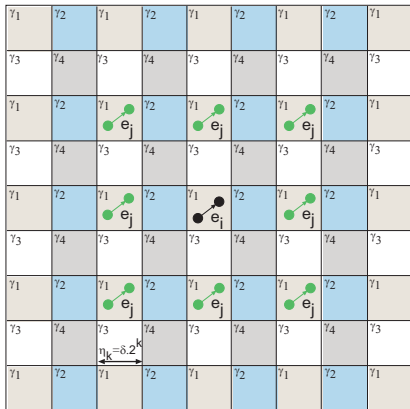
- Show that the **cumulative interference** I_{r_i} caused by concurrent transmissions from **all non-adjacent** cells is still within β

Approximation Algorithm in SINR



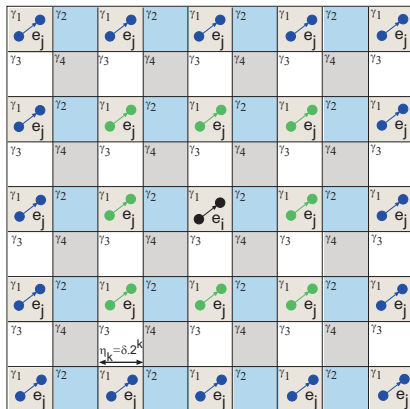
- Consider edge $e_i = (s_i, r_i) \in E_k$

Approximation Algorithm in SINR



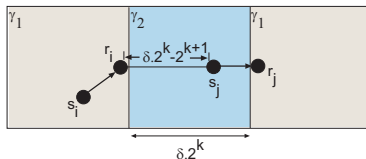
- Consider edge $e_i = (s_i, r_i) \in E_k$
- At most 8 from layer 1

Approximation Algorithm in SINR



- Consider edge $e_i = (s_i, r_i) \in E_k$
- At most **8** from **layer 1**
- At most **16** from **layer 2**, ..., at most **8q** from **layer q**
- Add up all the interferences up to **layer ∞**

Approximation Algorithm in SINR

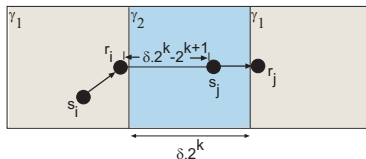


Computing Cumulative Interference I_{r_i}

- From transmitter s_j in a **layer 1** non-adjacent cell of the same color

$$I_{r_i}(s_j) = \frac{P}{\ell_{ij}^\alpha} \leq \frac{P}{[2^k(\delta - 2)]^\alpha}, \quad \because \ell_{ij} \geq \delta \cdot 2^k - 2^{k+1}$$

Approximation Algorithm in SINR



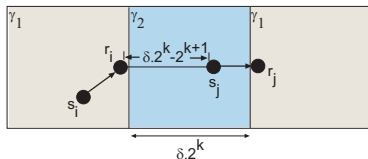
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- In general, $\ell_{ij} \geq 2^k \{(2q - 1)\delta - 2\}$ in **layer q**

Approximation Algorithm in SINR



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- In general, $\ell_{ij} \geq 2^k \{(2q - 1)\delta - 2\}$ in **layer q**
- Adding up

$$I_{r_i} \leq \sum_{q=1}^{\infty} \frac{8qP}{[2^k \{(2q - 1)\delta - 2\}]^\alpha} = \frac{8P}{2^{(k-1)\alpha} \delta^\alpha} \cdot \frac{\alpha - 1}{\alpha - 2} \leq \frac{P_{r_i}(s_i)}{\beta}$$

Approximation Algorithm in SINR

Theorem : $O(g(E_T))$ Approximation

Given a routing tree T on an arbitrarily deployed connected network in 2-D, and K orthogonal frequencies, the algorithm gives a $O(g(E_T))$ approximation on the optimal schedule length.

Approximation Algorithm in SINR

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Given a routing tree T on an arbitrarily deployed connected network in 2-D, and K orthogonal frequencies, the algorithm gives a $O(g(E_T))$ approximation on the optimal schedule length.

Proof Sketch

- Choice of the **critical cell** \hat{c} in which the number of edges on the **same frequency** $L_{\hat{c}}^{m*}$ is maximum across **all length classes**
- Show that OPT will take at least $L_{\hat{c}}^{m*} / \mu$ slots, for

$$\mu = \frac{[2(\sqrt{2} \cdot \delta + 1)]^\alpha}{\beta}$$

- Show by **contradiction** that OPT cannot schedule $\mu + 1$ edges on the **same frequency** in any cell

Approximation Algorithm in SINR

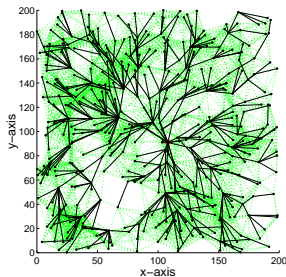
Proof Sketch (cobmining together)

$$\begin{aligned}\Gamma &\leq 4 \cdot \max_{k,c} \{|\gamma_{c \in C_k}|\} \cdot g(E_T) \\ &\leq 8 \cdot \max_{k,c} \left\{ L_{c \in C_k}^\phi \right\} \cdot g(E_T) \\ &\leq 8 \cdot \max_{k,c} \left\{ \left(\frac{4}{3} - \frac{1}{3K} \right) \cdot L_{c \in C_k}^{m*} \right\} \cdot g(E_T) \\ &\leq 8\mu \cdot \left(\frac{4}{3} - \frac{1}{3K} \right) \cdot g(E_T) \cdot OPT \\ &= O(g(E_T))\end{aligned}$$

Outline

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 - Motivation and Preliminaries
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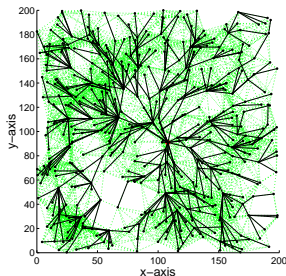
Properties of Spanning Trees



Shortest Path Tree (shallow and fat)

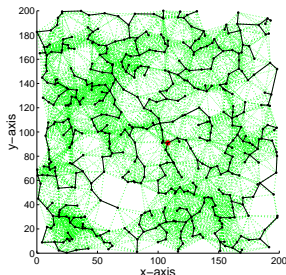
- High node degree \Rightarrow low throughput
- Few hops \Rightarrow low delay

Properties of Spanning Trees



Shortest Path Tree (shallow and fat)

- High node degree \Rightarrow low throughput
- Few hops \Rightarrow low delay



Minimum Interference Tree (weighted MST) [Mobihoc '04] (deep and skinny)

$w(u, v)$: no. of nodes covered by the union of two disks centered at u and v , each of radius $|uv|$

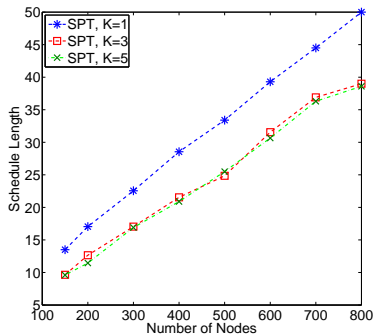
- Low node degree \Rightarrow high throughput
- More hops \Rightarrow high delay

Evaluation of \mathcal{A}_{UDG} on SPT & MIT

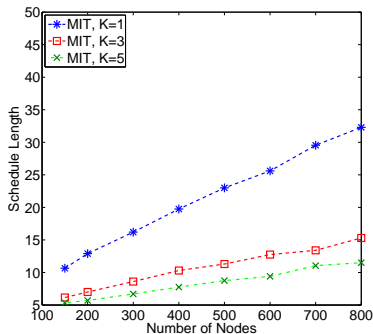
Parameters

Random geometric graph on a region of size 200×200 with $R = 25$

Shortest Path Tree



Minimum Interference Tree



Tree Property for Bounded Throughput

Theorem

If the **maximum node degree** of the routing tree is bounded by a **constant** $\Delta_C > 0$, then there exists an algorithm that gives a **constant factor** $8\mu_\alpha \cdot \Delta_C$ approximation on the optimal schedule length, where $\mu_\alpha > 0$ is a constant for a given cell size $\alpha \geq 2R$ and given node deployment.

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Properties

- Degree-bounded spanning trees? **Minimum Degree Spanning Tree** is NP-hard [SODA'92]
- Is **constant factor** approximation on **schedule length** and **delay** achievable?

Bicriteria Formulation

Bounded-Degree Minimum-Radius Spanning Tree

$\mathcal{P} = (\text{Degree, Radius, Spanning Tree})$

Radius: $R(T)$: Maximum hop distance from any node to sink in T

Δ^* : Budget on max degree

Goal: Find a spanning tree of **min radius** subject to **max degree** Δ^*

Bicriteria Formulation

Bounded-Degree Minimum-Radius Spanning Tree

$\mathcal{P} = (\text{Degree, Radius, Spanning Tree})$

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Goal: Find a spanning tree of **min radius** subject to **max degree** Δ^*

Approximation Definition

Algorithm \mathcal{A} is an (α, β) -approximation to a bicriteria optimization problem $\mathcal{P} = (\text{Degree, Radius, Spanning Tree})$ if:

- $\Delta(T) \leq \alpha + \Delta^*$
- $R(T) \leq \beta \cdot R^*(T)$

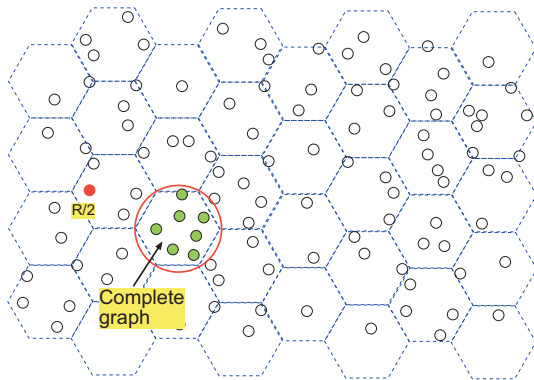
where $R^*(T)$ is the min radius of any spanning tree T whose max degree is Δ^* .

Algorithm Overview

Algorithm \mathcal{A}_{BDMRST}

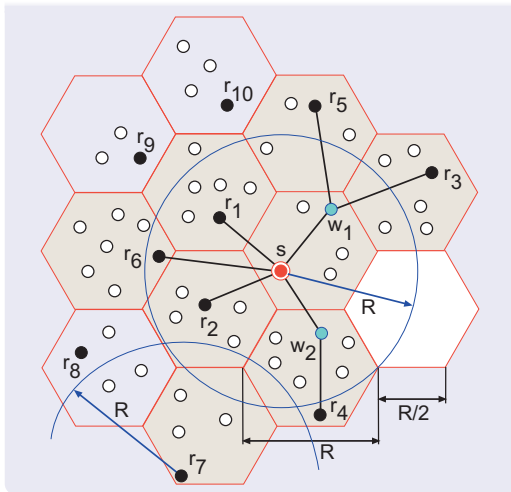
Three phases:

- 1 Construct a **Global Backbone Tree** of **low radius**.
- 2 Construct **degree-bounded Local Spanning Trees**.
- 3 **Merge** the local spanning trees and the global backbone tree.



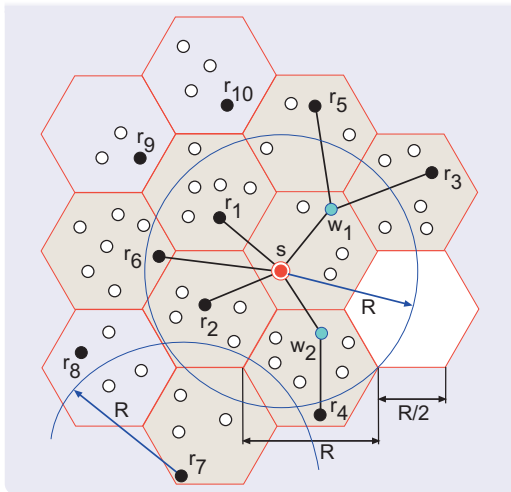
Algorithm Overview

Global Backbone Tree

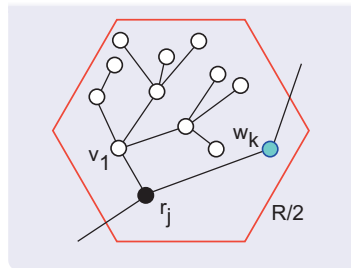


Algorithm Overview

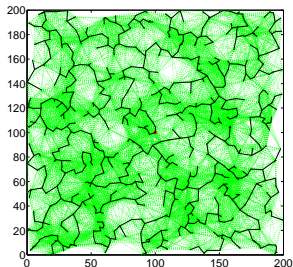
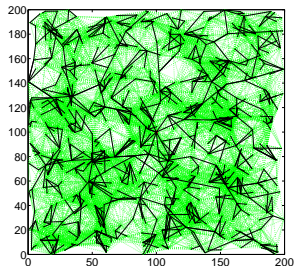
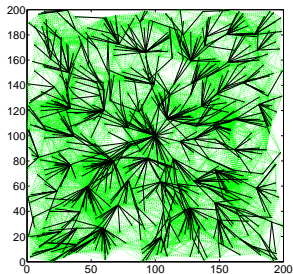
Global Backbone Tree



Local Spanning Tree



Properties of Spanning Trees



Bounded-Degree Minimum-Radius
Spanning Tree, $\Delta^* = 4$

Approximation Result & Evaluation

Theorem

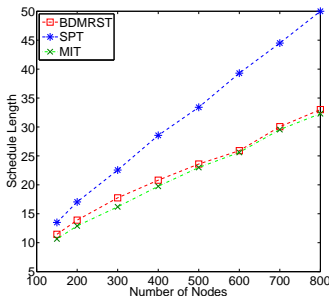
Algorithm \mathcal{A}_{BDMRST} gives a **constant factor** (α, β) bicriteria approximation for the **Bounded-Degree Minimum-Radius Spanning Tree**, where $\alpha = 10$ and $\beta = 5$.

Approximation Result & Evaluation

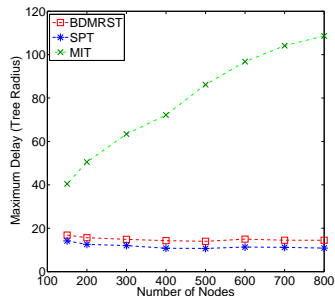
Theorem

Algorithm \mathcal{A}_{BDMRST} gives a **constant factor** (α, β) bicriteria approximation for the **Bounded-Degree Minimum-Radius Spanning Tree**, where $\alpha = 10$ and $\beta = 5$.

Schedule Length



Max Delay



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Contributions

- Maximizing aggregated convergecast throughput using **multi-channel scheduling**
 - **Constant factor** approximation on UDG
 - $\Delta(T) \cdot \log(n)$ approximation on DG
 - $O(g(E_T))$ approximation in SINR
- **Throughput-delay** trade-off in the same optimization framework
 - **Bicriteria** formulation
 - **Constant factor** approximation on constructing **bounded-degree minimum-radius spanning trees**
- Efficient, distributed **topology control in 3-D**
 - Simple **orthographic projection** based approach extending 2-D results
 - Robust **spherical Delaunay triangulation** based algorithm

Publications

Book Chapters

- 1 O.D. Incel, A. Ghosh, and B. Krishnamachari, [Scheduling Algorithms for Tree-Based Data Collection in Wireless Sensor Networks](#), Theoretical Aspects of Distributed Computing in Sensor Networks, Springer, 2010.
- 2 A. Ghosh and S.K. Das, [Coverage and Connectivity Issues in Wireless Sensor Networks](#), Mobile, Wireless and Sensor Networks: Technology, Applications and Future Directions, John Wiley & Sons, 2006.

Journal Papers

- 1 A. Ghosh, O.D. Incel, V.S. Anil Kumar, and B. Krishnamachari, [Multi-Channel Scheduling and Spanning Tree Algorithms: Throughput-Delay Trade-off for Fast Convergecast in Sensor Networks](#), ACM/IEEE Transactions on Networking, Feb 2010 (sub).
- 2 O.D. Incel, A. Ghosh, B. Krishnamachari, and K. Chintalapudi, [Fast Data Collection in Tree-Based Wireless Sensor Networks](#), IEEE Transactions on Mobile Computing, Dec 2009 (rev).
- 3 A. Viswanath, P. Dutta, M. Chetlur, P. Gupta, S. Kalyanaraman, and A. Ghosh, [Perspectives on Quality of Experience for Video Streaming over WiMAX](#), ACM SIGMOBILE Mobile Computing and Communications Review, Oct, 2009.
- 4 A. Ghosh and S.K. Das, [Coverage Connectivity Issues in Wireless Sensor Networks: A Survey](#), Journal of Pervasive and Mobile Computing, 4(3):303-334, June 2008.

Publications

Conference Papers (reverse chronologically)

- 1 A. Ghosh, R. Jana, V. Ramaswami, J. Rowland, and N.K. Shankar, [Modeling and Characterization of Large-Scale Wi-Fi Traffic in Public Hot-Spots](#), IEEE INFOCOM, 2011 (sub).
- 2 A. Ghosh, O.D. Incel, V.S. Anil Kumar, and B. Krishnamachari, [Optimal Spanning Trees for Fast Data Collection in Sensor Networks](#), IEEE INFOCOM Student Workshop, Mar 2010.
- 3 A. Ghosh, O.D. Incel, V.S. Anil Kumar, and B. Krishnamachari, [Multi-Channel Scheduling Algorithms for Fast Aggregated Convergecast in Sensor Networks](#), IEEE MASS, October 2009.
- 4 S.W. Lee, D. Yoon, and A. Ghosh, [Intelligent Parking Lot Application using Wireless Sensor Networks](#), International Symposium on Collaborative Technologies and Systems (CTS), May 2008.
- 5 A. Ghosh, L. Pereira, T. Yan, and H. Cao, [Modeling Wireless Sensor Network Architectures using AADL](#), European Congress on Embedded Real Time Software (ERTS), Jan 2008.
- 6 A. Ghosh, Y. Wang, and B. Krishnamachari, [Efficient Distributed Topology Control in 3 Dimensional Wireless Networks](#), IEEE SECON, Jun 2007.
- 7 A. Ghosh and S.K. Das, [A Distributed Greedy Algorithm for Connected Sensor Cover in Dense Sensor Networks](#), IEEE/ACM DCOSS, Jul 2005.
- 8 A. Ghosh, [Estimating Coverage Holes and Enhancing Coverage in Mixed Sensor Networks](#), IEEE LCN, Nov 2004.
- 9 S.K. Ghosh and A. Ghosh, [A Plan-Commit-Prove Protocol for Secure Verification of Traversal Path](#), IEEE International Conference on Networks (ICON), Nov 2004.

Manuscripts

- 1 T. Fu, A. Ghosh, E.A. Johnson, and B. Krishnamachari, [Energy-Efficient Deployment Strategies in Structural Health Monitoring using Wireless Sensor Networks](#), Structural Control and Health Monitoring, 2009 (manuscript).
- 2 A. Ghosh, A.H. Patel, C.R. Sastry, [Radio Frequency-Based Localization in Wireless Sensor Networks](#), Siemens Corporate Research Technical Report, Aug 2009.

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- **Siemens Corporate Research:** Chellury Ram Sastry
- **Microsoft Research:** Krishnakant Chintalapudi
- **Eaton Corporation:** Ting Yan, Luis Pereira, Hui Cao
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Thank You!