

Lecture 1 May 18, 2016

Office hours: M W after class

RTH 410 W 10am-12pm

bkrishna@usc.edu.

What this course is about

- Physical Layer: modulation, coding, radio propagation,

multipath fading, Delay/Doppler spread, MIMO, OFDM, CDMA, etc.

- Link Layer - Medium Access: randomized access - ALOHA, CSMA

scheduled access - TDMA/FDMA

Graph Theory - Graph coloring algorithms

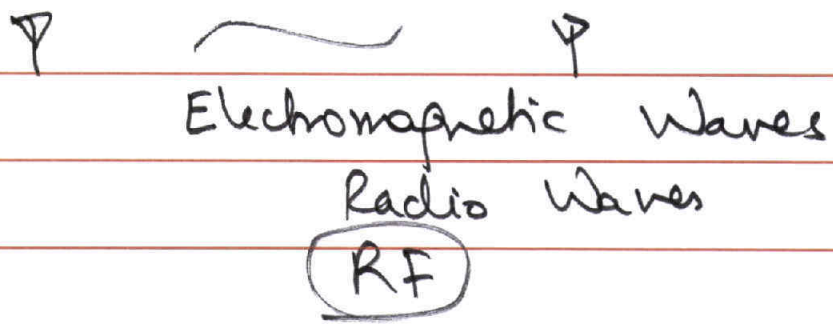
- Network Layer : Routing in multi-hop wireless networks such as wireless sensor networks / low power IoT networks or mesh networks
routing metric
mobile ad hoc networks
intermittently connected mobile networks

- Transport Layer : Congestion control
Utility based Network Optimization using Backpressure Scheduling.

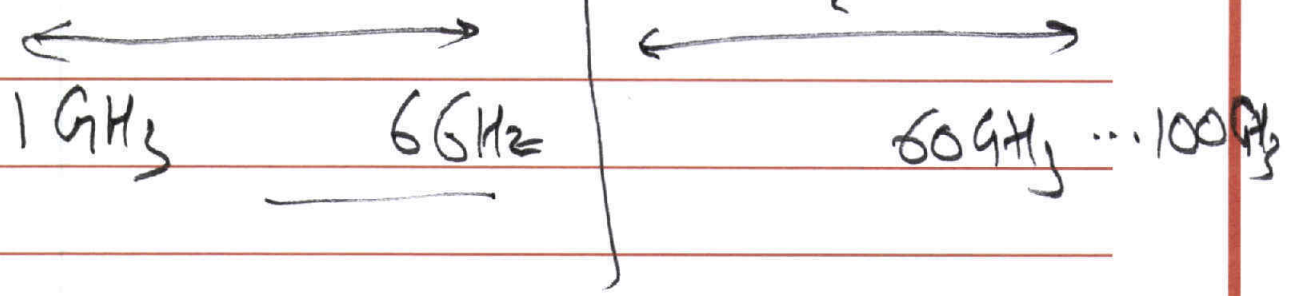
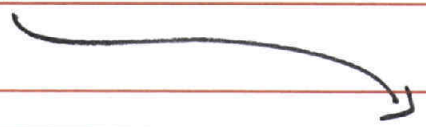
- Application Layer : mobile browsing, publish-subscribe middleware

Examples of current standards & protocols.

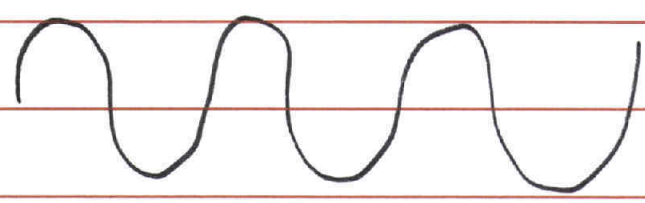
Physical Layer.



mm Wave



Sinusoidal signal.



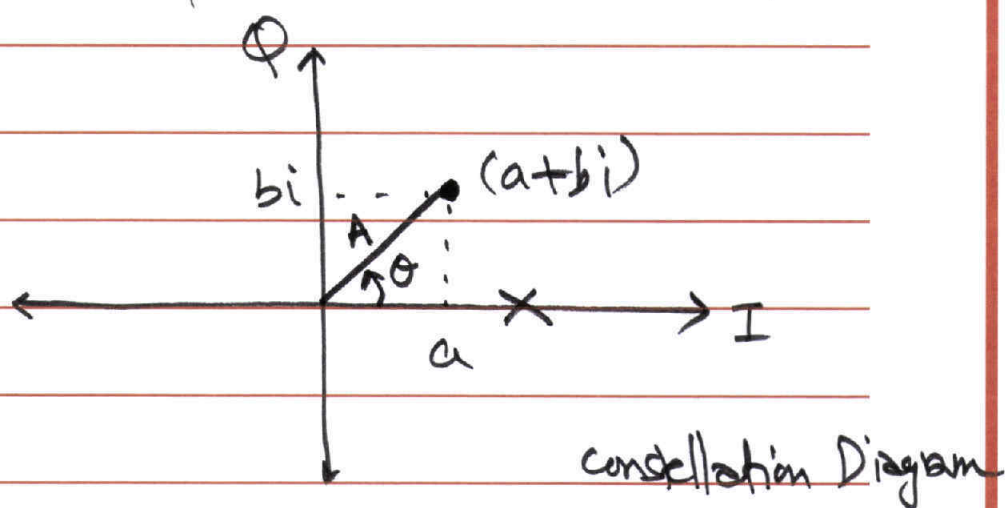
Carrier Wave.

$$A \sin(2\pi ft + \theta)$$

↑ ↑ ↑
 amplitude freq phase

fix the carrier frequency f_c

can vary amplitude & phase



Complex Plane

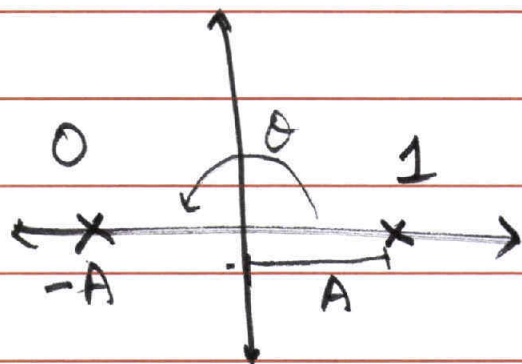
$$\underbrace{a}_{\text{Re}} + \underbrace{bi}_{\text{im}}$$

Argand Plane

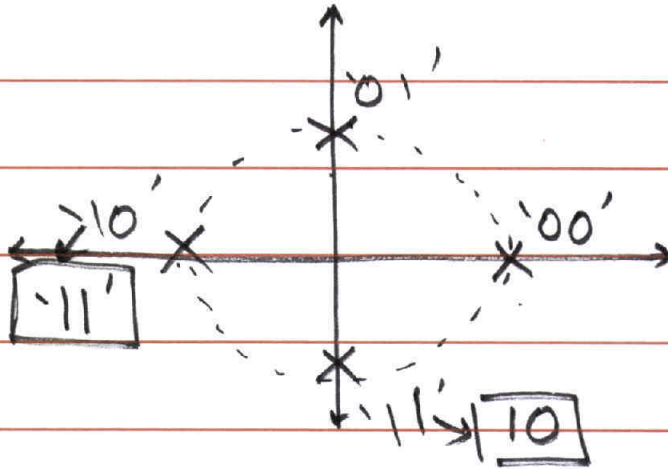
$$A, \theta$$

$$A = \sqrt{a^2 + b^2}$$

$$\theta = \tan^{-1}\left(\frac{b}{a}\right)$$

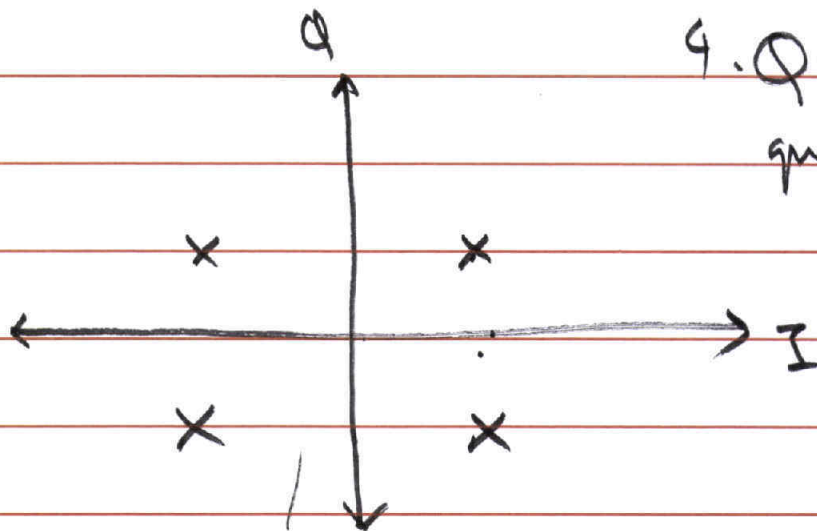


Binary Phase Shift Keying

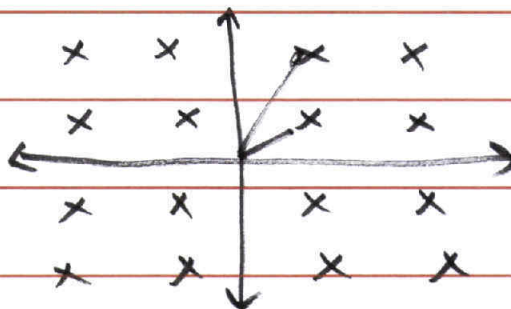


4 PSK
2 bit/symbol

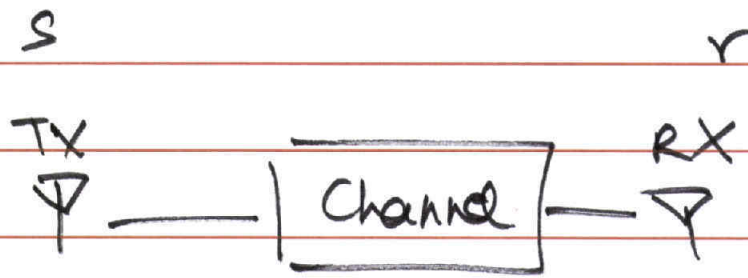
8 PSK
- 3 bit/symbol



4-QAM
quadrature
amplitude
modulation



16-QAM
4 bit/symbol



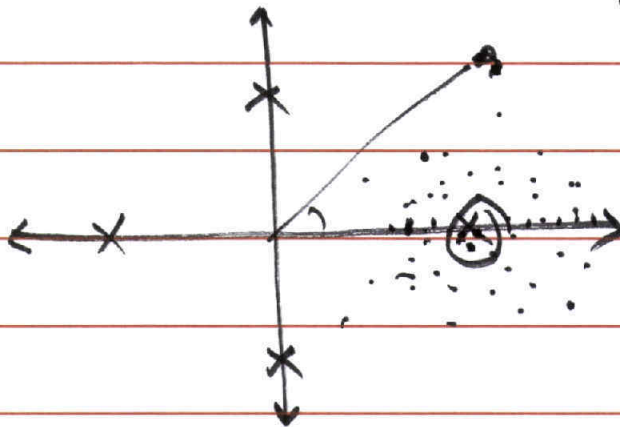
AWGN channel.

Additive white Gaussian Noise.

$$\underline{r} = \underline{s} + \underline{w}$$

\underline{r} : complex valued received signal
 \underline{s} : complex valued signal
 \underline{w} : Random noise

circularly symmetric
Complex Gaussian r.v.

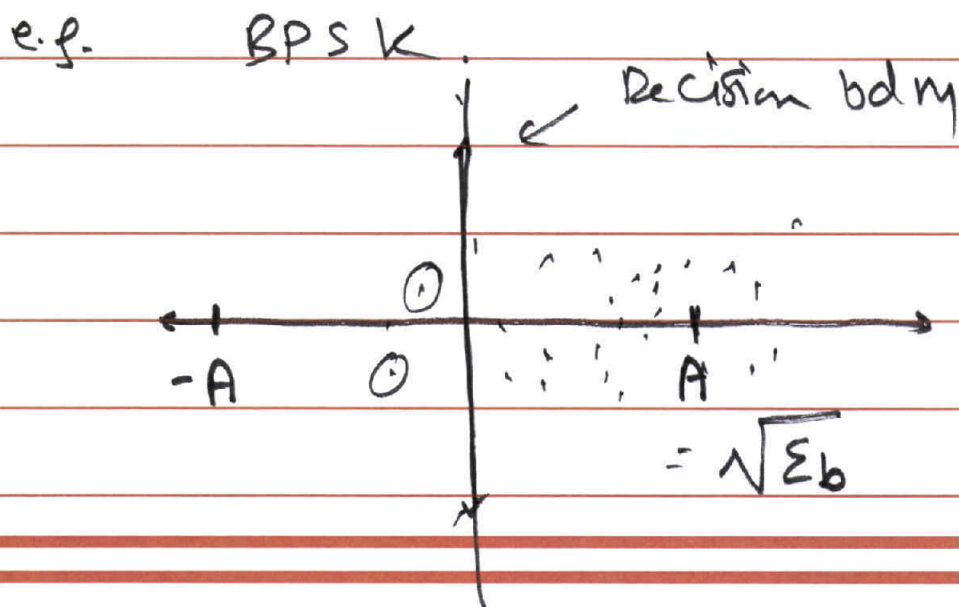


$$\underline{w} = \underline{r} - \underline{s} \text{ is also complex.}$$

$$= \underline{w}_{re} + \underline{w}_{im} \cdot i$$

w_{re} & w_{im} are both real Gaussian r.v. w/ zero mean & same variance. indep. of each other.

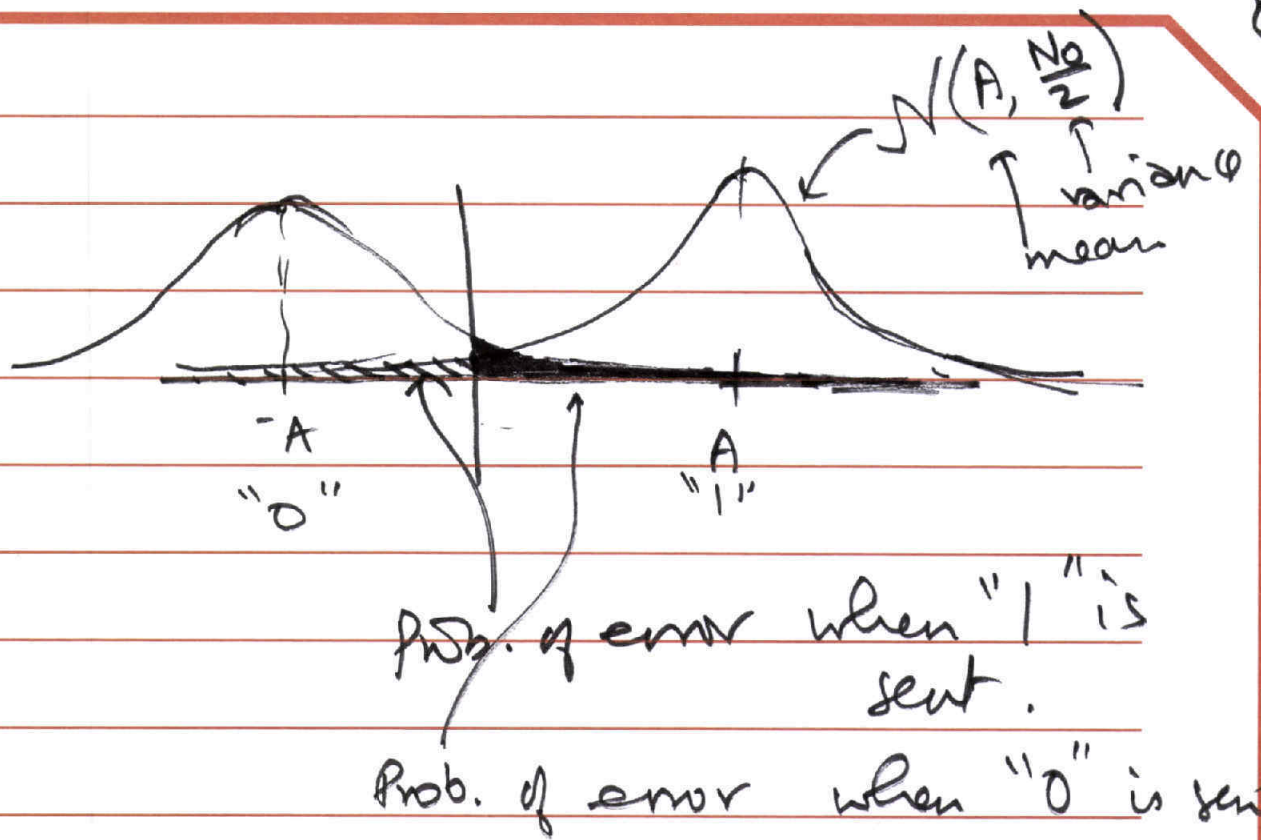
How do modulation schemes perform under AWGN?



What is the prob. of error?

total noise variance of N_0

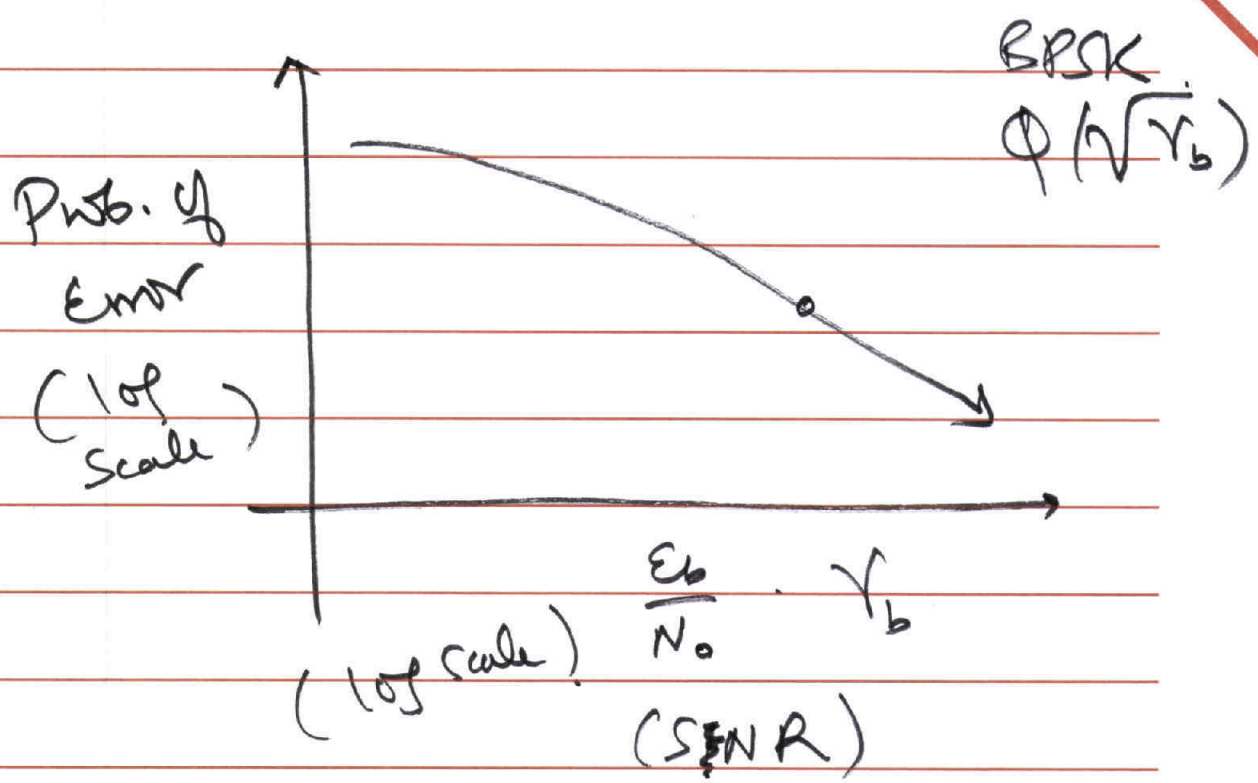
$$\text{Var. for } w_{re} = \text{var } w_{im} \\ = \frac{N_0}{2}$$



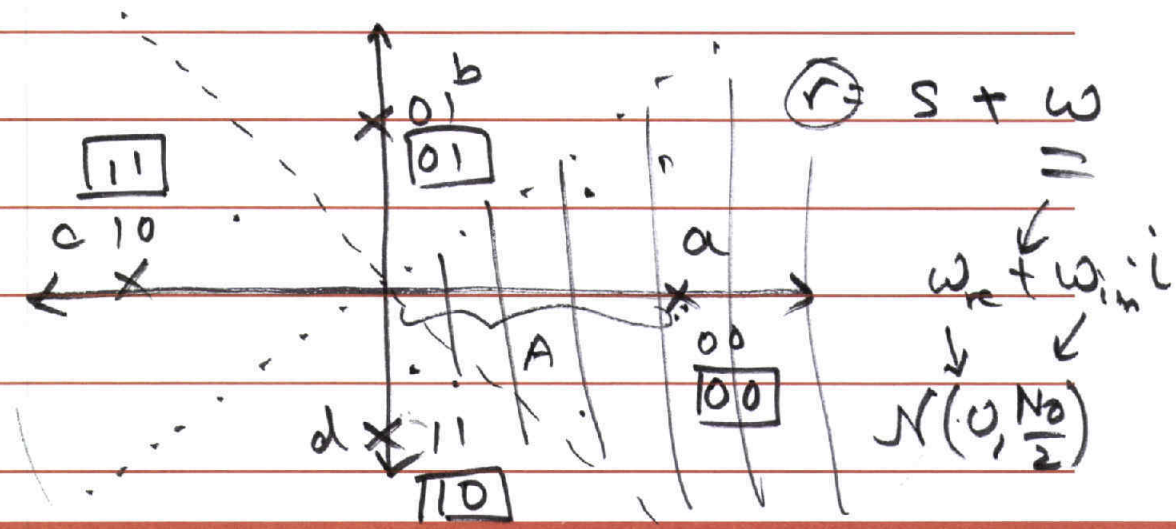
Q-function

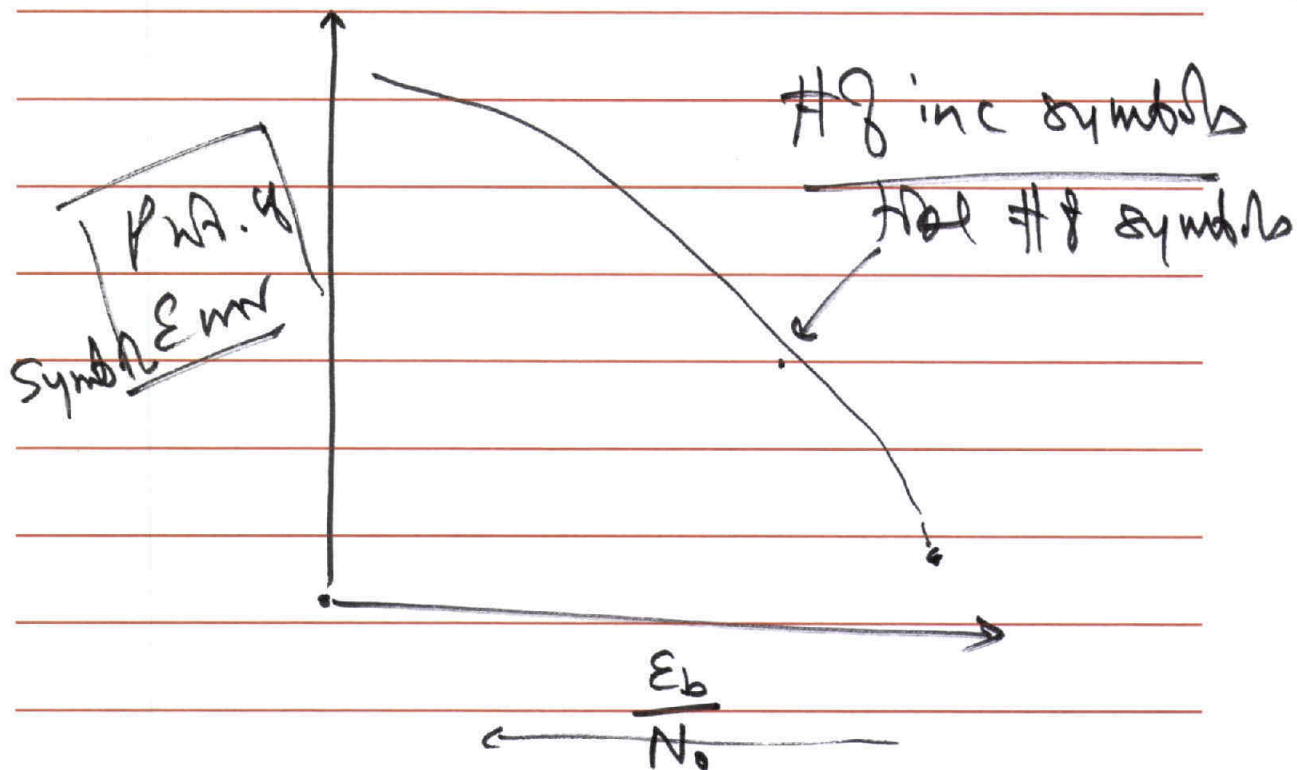
\int
 1 - cdf for Gaussian with
 mean 0 & std. dev. $\sqrt{\text{variance}}$

$$\begin{aligned}
 Q\left(\frac{A}{\text{std dev.}}\right) &= Q\left(\frac{\sqrt{E_b}}{\sqrt{\frac{N_0}{2}}}\right) \\
 &= Q\left(\sqrt{\frac{2E_b}{N_0}}\right) = Q(\sqrt{2\gamma_b})
 \end{aligned}$$



Compute numerically the
 Prob. of error for
 4-QPSK 4PSK



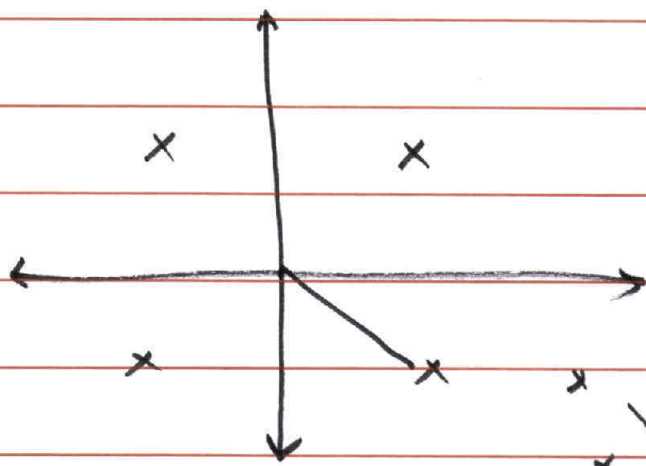


Try both encoding schemes
(regular & Gray encoding)
& see what happens to
the Bit Error Rate
(BER)

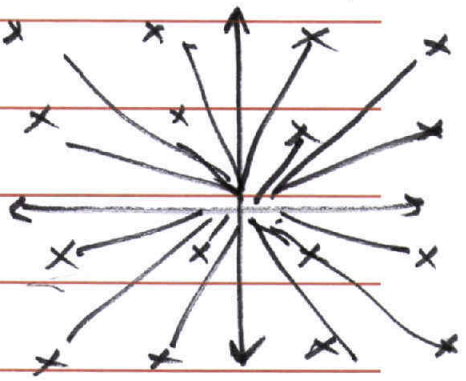
$$\frac{\# \text{ of incorrect bits}}{\text{total } \# \text{ of bits}}$$

how many symbols to send?

4 QAM



16 QAM



Rate & error rate

tradeoff.

Higher constellation Rate \uparrow
 for the same average energy,
 error rate \uparrow

for the same error rate,
 can get a higher data
 rate by using a larger constellation
 by doing _____.

to go from 4 QAM - 16 QAM
 & keep same error rate,
 need $\sim 4 \times$ the power
 for $2 \times$ improvement
 in rate

need to scale power
 exponentially to get

imp. in rate.

rate $\propto \log(1 + \text{power})$
 for fixed error rate.

$$R = B \log_2(1 + \text{SNR})$$

Rate - Power - Error Rate

A. fundamental tradeoff