

Medium Access.

Randomized Access

- slotted Aloha
- CSMA

Scheduled Access

- TDMA
- channelized protocols

Slotted Aloha: max throughput  
 $p^* = \frac{1}{n} \rightarrow \frac{1}{e}$

$\approx 36-37\%$

throughput regions if multiple users w/ different access probabilities

at the boundary  $\sum p_i^* = 1$

$$T_i = p_i \prod_{j \neq i} (1 - p_j)$$

CSMA : p CSMA ← p-persistent CSMA

Contention slots  $\delta \leq T_c \leq T_s$

$$\text{Throughput} = \frac{T_s n p (1-p)^{n-1}}{\delta \cdot (1-p)^n + T_s n p (1-p)^{n-1} + T_c \left( \frac{1 - (1-p)^n}{n p (1-p)^{n-1}} \right)}$$

802.11 CSMA → FSM describing the backoff stage & counter value

modelled as a Markov Chain

derive steady state probabilities

approximate as pCSMA.

for larger products CSMA throughput can be high 90% or more

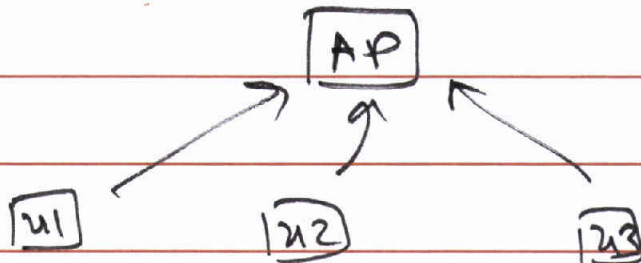
RACH channel in Cellular networks - control signalling channel - basically slotted Aloha

Scheduled access.

channelized systems

Channel : {  
- Time  
- Frequency  
- codes (CDMA)

orthogonal dimensions  
(ideally) → no interference.

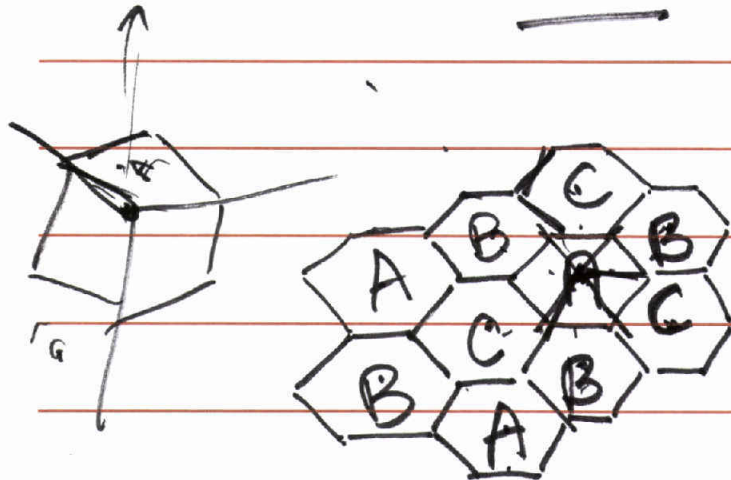


with Synchronization,  
nodes  
can be  
preallocated  
a  
time slot.

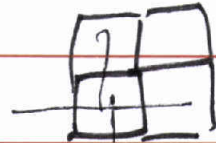
many applications, e.g. industrial  
sensing, have predictable,  
periodic traffic.

Another example: AMR

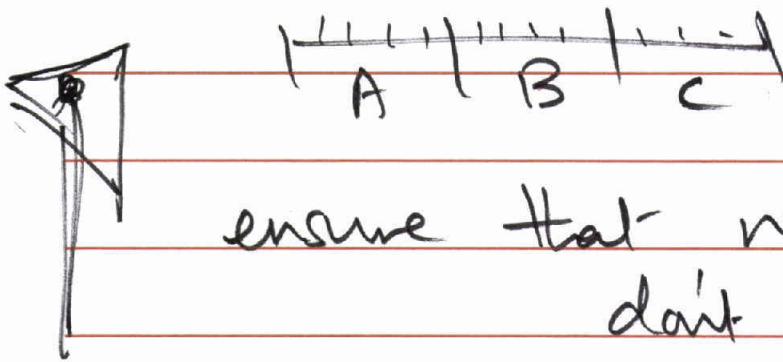
# Classic Cellular (Ideal)



- Tessellation
- Equidistant



Frequency reuse .

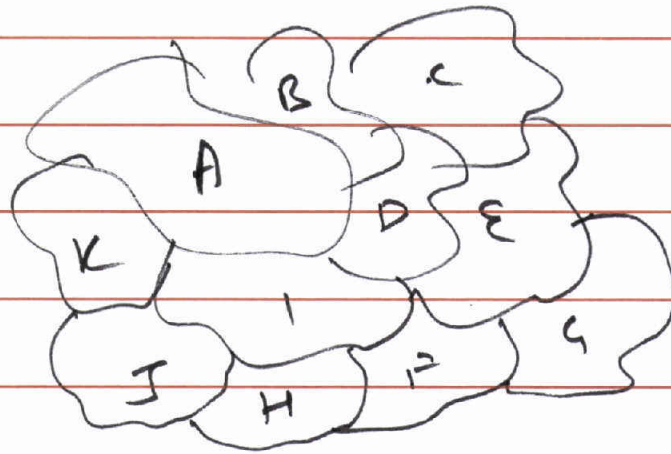


ensure that neighbor cells  
don't have the same  
channels,

but "far away" cells can  
reuse frequencies.

multi-sector cellular

An Arbitrary cellular system

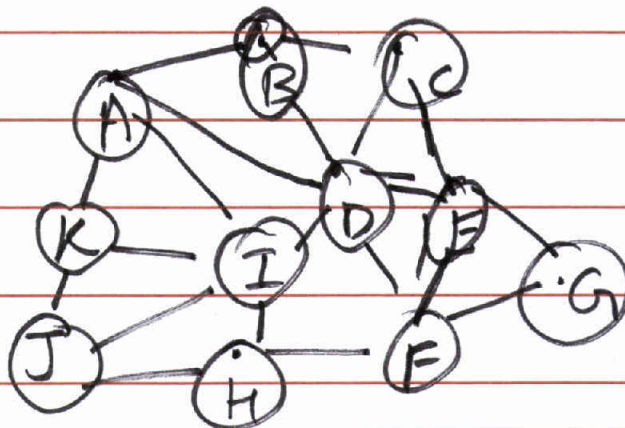


model the interference structure  
as a Graph.

$$G = (V, E)$$

cells  $\iff$  vertices

interfering cells have an edge between them.



1. how many "chunks" should the spectrum be divided into?
2. which chunk to allocate to which cell to ensure neighboring cells do not interfere?

Well known problem in Graph Theory:  
Vertex Coloring  
(Graph Coloring)

Try to allocate a set of colors, ~~to~~ one to each node / vertex, so that no two vertices sharing an edge have the same color, & minimize the number of colors used.

↓  
fewer "chunks"  $\Rightarrow$  more spectrum per cell.  $\Rightarrow$  more capacity / users per cell.

This problem (Vertex coloring)  
is NP-Hard.

Some problems such as  
shortest path ~~minim~~ can  
be solved exactly in  
time that scales polynomially  
in the problem size:

e.g. Dijkstra's ~~blus~~  $O(N^2)$   
w/ a simple implementation  
 $\sim O(|E| + |V| \log |V|)$   
more clever implementation

These problems are considered  
to be tractable or efficiently  
solvable.

said to be in the class P

For other problems, such as the longest-path routing problem, there are no known polynomial-time algorithms.

(~~so~~ instead exact algorithms take exponential ~~time~~ time:

$$O(2^{|V|})$$

These problems are called NP-Hard.

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⇒ cannot guarantee exact solution quickly always.

For many practical problems, can use heuristics that are fast, and often give exact

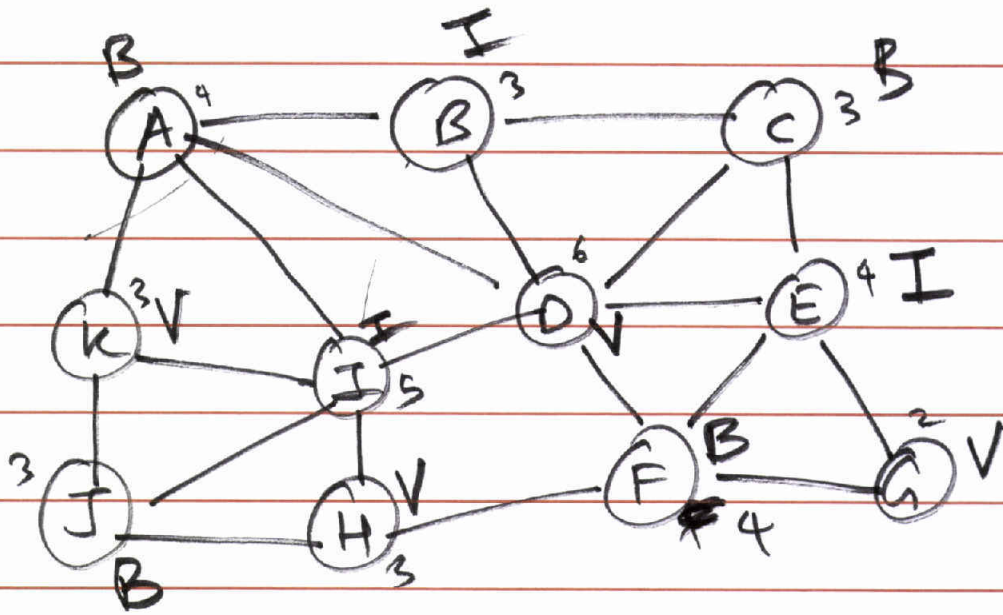


optimal OR near-optimal solutions.

A Heuristic algorithm for Graph vertex coloring:

Greedy Vertex Degree Ordering (GVDO) heuristic:

1. Sort vertices in decreasing order of their degree (i.e. # of neighboring vertices)
2. From the top of this list, assign the earliest possible color (reusing if possible) that does not violate the edge constraint



D I A E F B C H J K G

only  
3 colors needed!

- Violet
- Indigo
- Blue
- Green
- yellow
- orange
- Red
- ⋮
- ⋮

Optimal  
the number of colors needed  
is called the chromatic  
number of a graph  
 $\chi(G)$ .

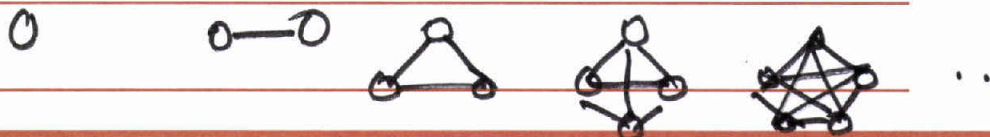
$$\chi(G) \leq \chi(G) \leq \Delta(G) + 1$$

max degree of graph  
↓

max

maximum  
clique size  
of graph.

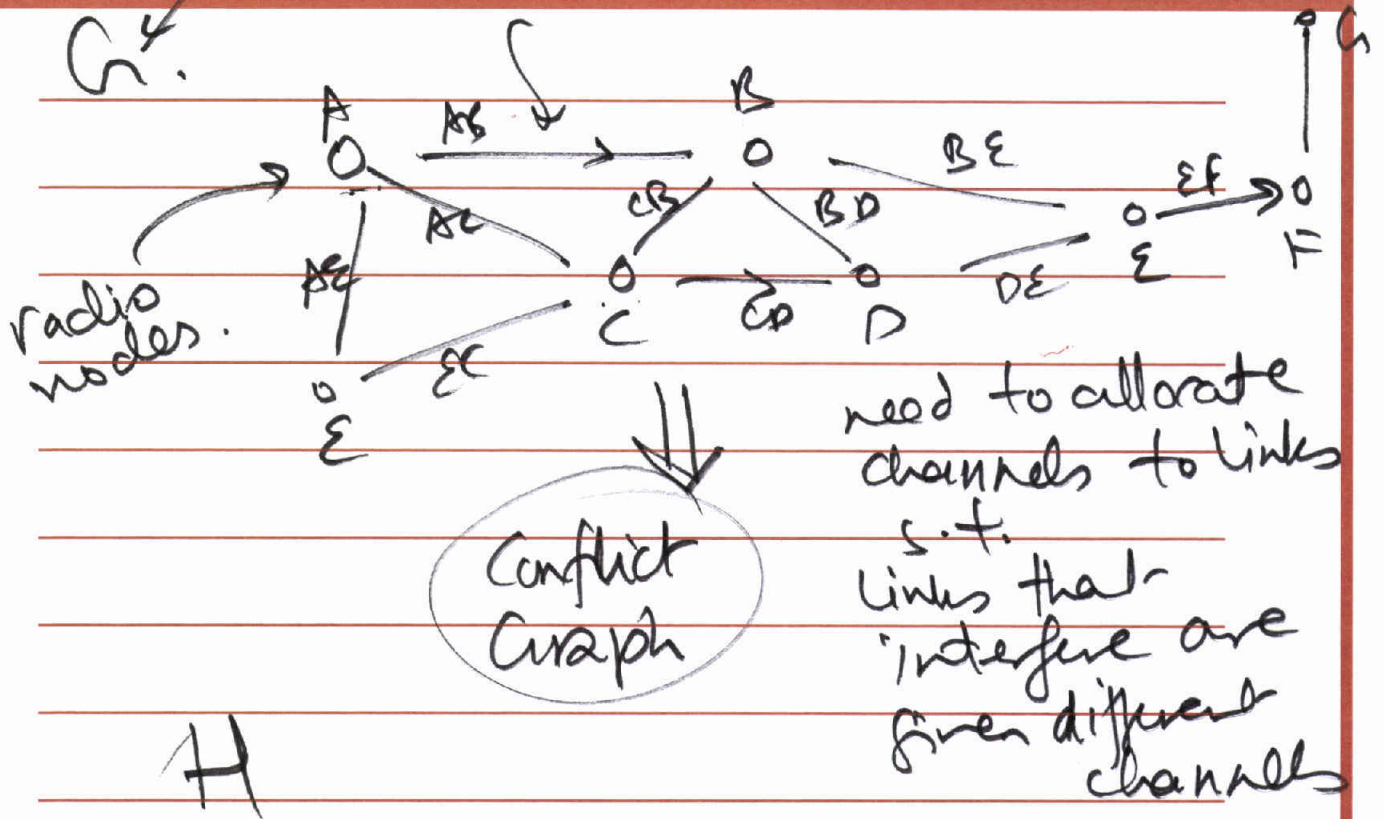
Clique: a <sup>sub-</sup>set  
of vertices that  
are all connected  
to each other



Can show that GVDG never  
needs more than  $\Delta(G) + 1$   
colors  
(maybe a loose bound).

Can apply graph coloring for allocating channels to links in multi-hop wireless networks such as low power IoT networks / mobile ad-hoc networks / wireless mesh networks.

Communication graph. wireless comm links



# Conflict Graph

node of  $H \iff$  link in  $G$

edges of  $H \iff$  pairs of links that cannot be operated in same channel

Vertex coloring on  $H \Rightarrow$  can use GVD for this

finds us the desired channel allocation on  $G$ .

fewer channels  $\Rightarrow$  higher throughput / capacity per link.