

# Static Replication Strategies for Content Availability in Vehicular Ad-hoc Networks

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**Abstract** This study investigates replication strategies for reducing latency to desired content in a vehicular peer-to-peer network. We provide a general constrained optimization formulation for efficient replication and study it via analysis and simulations employing a discrete random walk mobility model for the vehicles. Our solution space comprises of a family of popularity based replication schemes each characterized by an exponent  $n$ . We find that the optimal replication exponent depends significantly on factors such as the total system storage, data item size, and vehicle trip duration. With small data items and long client trip durations,  $n \sim 0.5$  i.e., a square-root replication scheme provides the lowest aggregate latency across all data item requests. However, for short trip durations,  $n$  moves toward 1, making a linear replication scheme more favorable. For larger data items and long client trip durations, we find that the optimal replication exponent is below 0.5. Finally, for these larger data items, if the client trip duration is short, the optimal replication exponent is found to be a function of the total storage in the system. Subsequently, the above observations are validated with two real data sets: one

based on a city map with freeway traffic information and the other employing encounter traces from a bus network.

**Keywords** data replication · availability · vehicular ad-hoc networks · optimization

## 1 Introduction

Advances in computer processing, data storage, and wireless communications have made it feasible to envision on-demand delivery of content such as audio and video clips between mobile vehicles. The content exchanged between the vehicles may vary from traffic information such as accident notifications and emergency vehicle arrival notifications to multimedia for entertainment such as audio files, cartoons, movies and other video files. A vehicle is equipped with an AutoMata (formerly known as a C2P2 for Car-to-Car Peer-to-Peer [10]) device consisting of several gigabytes of storage, a fast processor and a short-range wireless interface with bandwidths of several tens of Mbps [2]. The AutoMata-equipped vehicles, forming an intermittently connected network [23, 26], collaborate to realize an application for on-demand delivery of entertainment content.

In such a system, when a client vehicle issues a request for desired content not found in its local storage, this request can be satisfied only when it is in the vicinity of another vehicle that carries the requested item. Therefore, a key metric is availability latency, defined as the time between request issuance and request satisfaction. Clearly, the more the number of vehicles carrying a certain data item, the lower will be

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its expected availability latency. However, constraints on storage limit the number of unique data items that each vehicle can carry.

All data items in the system repository are not likely to be equally requested.<sup>1</sup> The aggregate availability latency across all items is therefore the average latency for individual data items weighed by their respective popularities. Hence, in order to minimize this aggregate latency metric, the popular data items warrant more replicas. We address the following key question in this study: how many replicas should be allocated for each item in the repository in order to minimize the aggregate availability latency?

Several parameters impact the optimal replication scheme. For instance, the mobility model of the vehicles impacts how the expected availability latency for a data item decreases with the number of replicas for that item. The size of a data item and the available bandwidth between devices dictates whether it is possible to download the entire data item in a single encounter between a client and a vehicle carrying the requested item. Moreover, the client trip duration bounds the maximum amount of time that a client is willing to wait for a request to be satisfied. The distribution of the data item popularities is a key component of the aggregate latency metric. The available storage directly affects the constraints under which the optimal replication strategy can be found.

Our primary contributions are as follows. We first provide a general optimization formulation for minimizing the average availability latency subject to a storage constraint per vehicle. To solve this optimization, the solution space we explore comprises a family of popularity-based replication schemes each characterized by an exponent  $n$ . This exponent,  $n$ , defines the relation between the replicas of a data item and its popularity. We are interested in the optimal replication exponent that minimizes the aggregate availability latency. With small data items and long client trip durations, we find that  $n \sim 0.5$  i.e., a square-root replication scheme provides the lowest aggregate latency. However, for short trip durations, we find that the optimal replication exponent ( $n$ ) moves toward 1, making a linear replication scheme more favorable. For larger data items and long client trip durations, we find that the optimal replication exponent is below 0.5. In the limit for extremely large data items, a random ( $n = 0$ ) replication scheme that allocates the same number of replicas to all data items yields the minimum aggregate

latency. Finally, for such data items, if the client trip duration is short, we find that the optimal replication exponent is a function of the total storage in the system. Specifically, in low storage scenarios, a linear scheme shows superior performance, while for moderate to high storage scenarios a square-root replication scheme is preferred. Moreover, if the storage is abundant even a random replication scheme is good enough to provide a low aggregate latency.

While the above results are based on a 2D random walk based mobility model for the vehicles, in the second part of this study, we validate our model observations with vehicular movements obtained from real data sets. Specifically, two independent validation phases are presented employing (a) A real map of an urban environment that dictates the mobility transitions of the Markov model and (b) Fine grained mobility traces from a real environment comprising buses moving around a university campus area. The observations from these studies indicate that a random walk-based mobility model captures performance trends that may be applicable for a wide range of scenarios.

The rest of this paper is organized as follows. Section 2 gives a brief overview of the related work in the area. Section 3 presents the general optimization formulation and details about the family of frequency-based replication schemes explored in our study. Section 4 employs mathematical analysis and simulations to determine the optimal replication scheme for small data items and long client trip durations. The results for small data items are extended to consider short client trip durations in Section 5. Sections 6 and 7 present the optimal replication scheme for larger data items with long and short client trip durations, respectively. Subsequently, representative results obtained with the random walk model are validated on a map of the city of San Francisco in Section 8 as well as a real data set comprising of movement traces of buses in a small neighborhood in Amherst (Section 9). Finally, Section 10 presents conclusions and future research directions.<sup>2</sup>

## 2 Related work

Techniques to determine number of replicas are similar to assigning seats to different parties as a function of their popularity, i.e., ratio of votes casted for a party to the total vote. Webster's divisor method and its alternatives attributed to Hamilton, Adams and

<sup>1</sup>It is found that Zipf's law controls many of the features observed with the Internet, primarily because of different user preferences for different files [3].

<sup>2</sup>A detailed technical report of this study is available as [22].

Jefferson allocate storage to each replica (assign seats to a party) as a linear function of its frequency of access (popularity). The divisor technique has been employed to determine the number of replicas of a video clip in a distributed video-on-demand architecture [27]. Our proposed framework captures this technique by setting a key parameter, denoted as  $n$  (see Section 3), to one.

Techniques to compute number of replicas for objects have been studied for both peer-to-peer networks [5] and mesh community networks [7, 11]. Mobility of nodes is our primary contribution and separates these prior studies from the work presented here. In the following, we provide an overview of these prior studies. Replication of objects is important to their discovery in an un-structured peer-to-peer network. A smart replication technique minimizes search size, defined as the number of walks required to locate a referenced data item. In [5], the divisor method is compared with one that employs the square root of the frequency of access, demonstrating the superiority of the later.

Replication in MANETs has been explored in a wide variety of contexts. Hara [13] proposes three replica allocation methods. The first one that allocates replicas to nodes only on the basis of their local preference to data items. The second technique extends the first by considering the contents of the connected neighbors while performing the allocation to remove some redundancy. The last technique discovers bi-connected components in the network topology and allocates replicas accordingly. The frequency of access to data items is known in advance and does not change. Moreover, the replica allocation is performed in a specific period termed the relocation period. Several extensions to this work have been proposed where replica allocation methods have been extended to consider data items with periodic [14, 15] and aperiodic [18] updates. Further extensions to the proposed replica allocation methods consider the stability of radio links [19], topology changes [20] and location history of the data item access log [16, 17].

Our study differs from prior studies in the following ways. We formulate a general optimization problem that minimizes an aggregate latency metric subject to a storage constraint per vehicle. We propose a family of replication schemes and explore which scheme provides optimal latency under a variety of scenarios by solving the optimization formulation. The mobility of vehicles is represented by a Markov-based mobility model that is general enough to capture a wide variety of mobility models such as Freeway, Highway, Random Way-point etc. We have analyzed the latency performance obtained with such a mobility model via mathematical analysis and extensive simulations. The different scenarios encompass vehicles with unbounded

as well as finite trip durations, data items with different display times etc.

### 3 General framework

In this section, we first introduce some definitions and associated terminology used repeatedly in this paper. Then, we provide a general optimization formulation for minimizing availability latency in the presence of storage constraints. Table 1 summarizes the notation used in this study.

Assume a network of  $N$  mobile AutoMata devices, each with storage capacity of  $\alpha$  bytes. The total storage capacity of the system is  $S_T = N \cdot \alpha$ . There are  $T$  data items in the repository, each with a display time of  $\Delta_i$  seconds and display bandwidth requirement of  $\beta_i$ . Hence, the size of each item is given by  $S_i = \Delta_i \cdot \beta_i$ . The frequency of access to item  $i$  is denoted as  $f_i$  with  $\sum_{j=1}^T f_j = 1$ . Let the trip duration of the client AutoMata under consideration be  $\gamma$ . We now define the normalized frequency of access to the item  $i$ , denoted  $R_i$ , is:

$$R_i = \frac{(f_i)^n}{\sum_{j=1}^T (f_j)^n}; 0 \leq n \leq \infty \tag{1}$$

$R_i$  is normalized to a value between 0 and 1. The number of replicas for data item  $i$ , denoted as  $r_i$ , is:

$$r_i = \min \left( N, \max \left( 1, \left\lfloor \frac{R_i \cdot N \cdot \alpha}{S_i} \right\rfloor \right) \right) \tag{2}$$

This defines a family of replication schemes that computes the degree of replication of item  $i$  as the  $n^{th}$  power of its frequency of access. The exponent  $n$  characterizes a particular replication scheme. Hence,  $r_i$  lies between 1 and  $N$ . Note that  $r_i$  includes the original copy of item  $i$ . One may simplify Eq. 2 by replacing the max function with  $\lfloor \frac{R_i \cdot N \cdot \alpha}{S_i} \rfloor$ , which would allow value of  $r_i$  to drop to zero. This means that there is no copy of item  $i$  in the AutoMata network. A hybrid framework might provide access to the item  $i$ . For example, a base station employing IEEE 802.16 [12] might facilitate access to a wired infrastructure with remote servers containing the item  $i$ . However, in this study, we assume at least one copy of every data item must be present in the ad-hoc network at all times.

The availability latency for a given request for item  $i$ , denoted as  $\delta_i$ , is defined as the time after which a client AutoMata will find at least one replica of its requested item accessible to it, either directly or via multiple hops. Additionally,  $\delta_i$  must be greater than  $\Delta_i$ , the data item display time. If a replica for item  $i$  is not encountered for a given request, we set  $\delta_i$  to  $\gamma$ . This

**Table 1** Terms and their definitions

Database Parameters	
$T$	Number of data items.
$S_i$	Size of data item $i$ .
$\Delta_i$	Display time of data item $i$ .
$\beta_i$	Bandwidth requirement of data item $i$ .
$f_i$	Frequency of access to data item $i$ .
Replication Parameters	
$R_i$	Normalized frequency of access to data item $i$ , $R_i = \frac{(f_i)^n}{\sum_{j=1}^T (f_j)^n}; 0 \leq n \leq \infty$
$r_i$	Number of replicas for data item $i$ , $r_i = \min(N, \max(1, \lfloor \frac{R_i \cdot N \cdot \alpha}{S_i} \rfloor))$
$n$	Characterizes a particular replication scheme.
$\delta_i$	Average availability latency of data item $i$
$\delta_{agg}$	Aggregate availability latency for replication technique using the $n^{th}$ power, $0 \leq n \leq \infty$ , $\delta_{agg} = \sum_{j=1}^T \bar{\delta}_j \cdot f_j$
AutoMata System Parameters	
$N$	Number of AutoMata devices in the system.
$\alpha$	Storage capacity per AutoMata.
$\gamma$	Trip duration of the client AutoMata.
$S_T$	Total storage capacity of the AutoMata system, $S_T = N \cdot \alpha$ .

indicates that item  $i$  was not available to the client during its journey. Also, if  $\Delta_i$  exceeds  $\gamma$  for a certain item  $i$  then we set  $\delta_i$  to  $\gamma$ . We are interested in the availability latency observed across all the data items. Hence, we augment the  $\delta_i$  for every item  $i$  with its  $f_i$ . This is termed the aggregate availability latency ( $\delta_{agg}$ ) metric. It is computed as follows. For each item  $i$ , calculate the average availability latency ( $\bar{\delta}_i$ ) based on the particular replication scheme of interest. Then these availability latencies are combined into a single metric:  $\delta_{agg} = \sum_{i=1}^T \bar{\delta}_i \cdot f_i$ .

The aggregate availability latency depends on the value chosen for  $n$ , since  $n$  determines the replicas per data item. Intuitively, a higher number of replicas for item  $i$  will reduce the availability latency for a request for that item. The core problem of interest here is to keep the aggregate availability latency as low as possible by tuning the data item replication levels, in the presence of storage constraints. We assume that the data item repository size is smaller than the total storage capacity of the system,  $\sum_{i=1}^T S_i \leq S_T$ . Otherwise, data items cannot be replicated when at least one replica of a data item must be present in the system. More formally, the optimization problem can be stated as,

$$\text{Minimize } \delta_{agg}, \text{ subject to } \sum_{i=1}^T S_i \leq S_T \tag{3}$$

Implicit in this formulation is the design variable, namely, the desired replication for each data item. The replication exponent  $n$  determines a  $r_i$  value for each data item  $i$  with the objective to minimize  $\delta_{agg}$ .

This minimization is a challenge when the total size of the database exceeds the storage capacity of a car,  $\sum_{i=1}^T S_i > \alpha$ . Otherwise, the problem is trivial and can be solved by replicating the entire repository on each device.

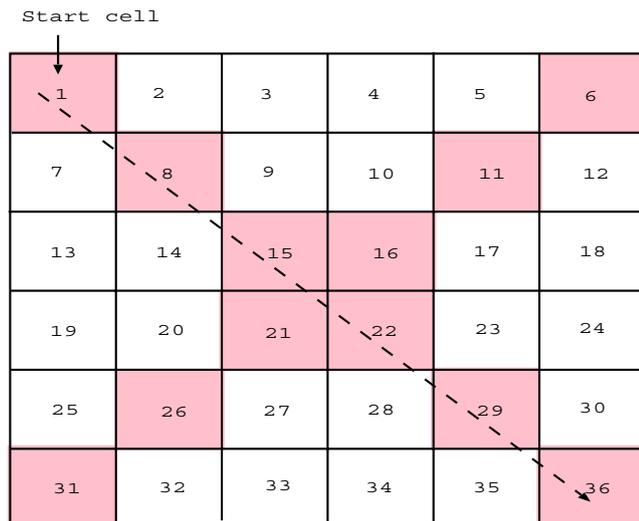
The optimization space that defines what value of  $n$  provides the best  $\delta_{agg}$  is quite large and consists of the following parameters: (i) density of cars, (ii) data item display time, (iii) data item size, (iv) display bandwidth per data item, (v) data item repository size, (vi) storage per car, (vii) client trip duration, (viii) frequency of access to the data items, and (ix) mobility model for the cars. In this study, we determine how the aggregate availability latency and hence the optimal replication scheme is affected by each of these parameters.

### 3.1 Model preliminaries

In this section, we provide details about the discrete Markov mobility model adopted in this study. We assume a repository of homogeneous data items with identical bandwidth requirement, display time, and size ( $\beta_i = \beta$ ,  $\Delta_i = \Delta$ ,  $S_i = S$ ). Figure 1 shows an example map used in our study that comprises with fixed size cells.<sup>3</sup> The vehicles<sup>4</sup> themselves are assumed to be distributed across these cells. Only AutoMatas within a

<sup>3</sup>In the analysis, the map is considered to be a torus to avoid border effects [21, 25].

<sup>4</sup>We use the term AutoMata and a vehicle (or car) interchangeably in this study, with the assumption that each vehicle is equipped with a single AutoMata device.



**Figure 1** An example  $6 \times 6$  map

cell communicate with each other either directly if they are in radio-range or via other AutoMata using multi-hop transmissions. In other words, the AutoMata within a cell form a connected sub-network. AutoMata in adjacent cells cannot communicate with each other.

A Markov mobility model describes the movement of the vehicles where the vehicles perform a 2D random walk. Hence, in each time step, a vehicle in a given cell may transition to any one of its neighboring 4 cells. Each cell of the map constitutes a state. A map of size  $G \times G$  yields  $G^2$  states. These states are self-contained and a transition from one state to another is independent of the previous history of a car in that state. The aggregate of the transitions from each cell (state) to every other state gives the  $G \times G$  probability transition matrix  $Q = [q_{ij}]$  where  $q_{ij}$  is the probability of transition from state  $i$  to state  $j$ .

Using Markov chains, it is possible to estimate the distribution of the steady-state probabilities of being in the various cells, by solving  $\Pi = \Pi * Q$ , where  $\Pi$  is the vector representing the steady-state probabilities of being in the various cells (states). While for the 2D random walk mobility model, due to symmetry and ignoring border effects,  $\Pi = \frac{1}{G}$ , in general, the map may represent an underlying city area where the transition probabilities for each cell may not be symmetric in each of the 4 possible directions. For example, in the example map depicted in Fig. 1, the mobility model is weighted toward the diagonal both from the left to right and vice-versa. This may be due to the presence of two major freeways running across a city area that the map represents. Note that in order to incorporate directionality, the transition for a vehicle from its current cell may incorporate the current as well as the previous

location of the vehicle (see Section 8). In this case, by incorporating previous as well as current vehicle location information in the state, the mobility model can still be solved employing Markov chains.

Without any loss of generality, to reduce the dimensionality of the problem, we express the data item display time,  $\Delta$ , as the amount of time required by an AutoMata equipped vehicle to travel  $\Delta$  cells. We express  $\alpha$  as the number of storage slots per AutoMata. Each storage slot stores a data item fragment equivalent to a single cell worth of data item display time. Moreover, we assume the amount of data displayed in each cell is identical. Now, we represent both the size of a data item and the storage slots in terms of the number of cells. This means that a data item has a display time of  $\Delta$  cells and an AutoMata has  $\alpha$  units of cell storage. For example, a data item with display time of 4 cells ( $\Delta = 4$ ) requires 4 storage slots and an AutoMata provides 100 storage slots ( $\alpha = 100$ ). Hence, from hereon, we assume that the size of the data item is indicated by its display time.

The trip duration ( $\gamma$ ) is the maximum amount of time that a client vehicle is willing to wait for request satisfaction. Here, it is expressed as the maximum number of cells that the client is willing to traverse before it gives up on a given request for a data item. We also define availability latency ( $\delta_i$ ) for data item  $i$  in discrete terms, as the number of cells after which a client AutoMata will encounter a replica of the requested data item  $i$ , either directly or via multiple hops, for the data item display time ( $\Delta$ ). Hence, the possible values of the availability latency are between 0 and  $\gamma$ . While in most cases, the trip duration is usually short, occasionally a client may specify an extremely large value of  $\gamma$  indicating that it is willing to wait as long as it takes to satisfy an issued request. As we shall show in the following sections, the long versus short client trip durations have a profound impact on the optimal replication scheme that minimizes the aggregate availability latency.

#### 4 Data items with small size and long client trip duration

In this section, we consider small data items with a display time of one, where the client trip duration is long. We first present analytical approximations that capture the performance of availability latency for an item as a function of the number of replicas for that item for both a low and high density of replicas. Subsequently, we employ simulations to determine the optimal replication exponent that minimizes the aggregate availability latency.

### 4.1 Analysis of data items with display time = one

In this section, for a scenario with a sparse density of data item replicas, we derive a closed-form expression for the aggregate availability latency. Subsequently, we use this expression to solve the optimization problem to reveal that a *square-root* replication scheme minimizes this latency. Then, we derive an expression that approximates the aggregate availability latency in case of a high density of data item replicas.

#### 4.1.1 Sparse scenario

In this section, we provide a formulation that captures scenarios with a low density of vehicles. For a given mobility model of the vehicles, the relationship between  $\delta_i$  and  $r_i$  can be obtained using simulations. For illustration, we have considered that vehicles follow a random walk-based mobility model on a 2D-torus. Aldous and Fill [1] show that the mean of the hitting time for a symmetric random walk on the surface of a 2D-torus is  $\Theta(G \log G)$  where  $G$  is the number of cells in the torus. Moreover, the mean of the meeting time for 2 random walks is half of the mean hitting time. Furthermore, the distribution of the meeting times for an ergodic Markov chain can be approximated by an exponential distribution of the same mean [1]. Hence,

$$P(\delta_i > t) = \exp\left(\frac{-t}{c \cdot G \cdot \log G}\right) \tag{4}$$

where the constant  $c \simeq 0.34$  for  $G \geq 25$ . Now since there are  $r_i$  replicas, there are  $r_i$  potential servers. Hence, the meeting time, or equivalently the availability latency for the data item  $i$  is the time till it encounters any of these  $r_i$  replicas for the first time. This can be modeled as a minimum of  $r_i$  exponentials. Hence,

$$P(\delta_i > t) = \exp\left(\frac{-t}{c \cdot \frac{G}{r_i} \cdot \log G}\right) \tag{5}$$

Note, however that this formulation is valid only for the cases when  $G \gg r_i$ , which is the case for sparse scenarios. The expected value of  $\delta_i$  is given by:

$$\bar{\delta}_i = \frac{c \cdot G \cdot \log G}{r_i} \tag{6}$$

For a given 2D-torus,  $G$  is constant, hence we have  $\bar{\delta}_i \propto \frac{1}{r_i}$  or equivalently,  $\bar{\delta}_i = \frac{C}{r_i}$  where  $C = c \cdot G \cdot \log G$ .

Hence, we have the following optimization formulation,

$$\text{Min} \left[ \sum_{i=1}^T f_i \cdot \frac{C}{r_i} \right] \text{ Subject to} \tag{7}$$

$$\sum_{i=1}^T r_i = N \cdot \alpha; 1 \leq r_i \leq N \forall i = 1 \text{ to } T \tag{8}$$

**Theorem 1** *The solution to the optimization formulation presented in Eqs. 7–8 is:*

$$r_i = \begin{cases} \frac{\sqrt{f_i \cdot N \cdot \alpha}}{\sum_{j=1}^T \sqrt{f_j}} & \frac{1}{N \cdot \alpha} \leq \frac{\sqrt{f_i}}{\sum_{j=1}^T \sqrt{f_j}} \leq \frac{1}{\alpha} \\ \max\left(1, \min\left(\sqrt{\frac{f_i \cdot C}{\gamma_0}}, N\right)\right) & \text{in the general case} \\ & \text{where } \gamma_0 \text{ is s.t.} \\ & \sum_{i=1}^T r_i = N \cdot \alpha \end{cases} \tag{9}$$

*In other words, in case of a sparse density of vehicles, a replication scheme that allocates data item replicas as a function of the square-root of the frequency of access to data items minimizes the aggregate availability latency. This is valid for data items with display time = 1.*

*Proof* We solve the above optimization using the method of Lagrange multipliers. First, we prove part(i) of the theorem.

The Lagrangian for the optimization can be written as:

$$H = \sum_{i=1}^T \frac{f_i \cdot C}{r_i} + \varphi \left[ \sum_{i=1}^T r_i - N \cdot \alpha \right] \tag{10}$$

We solve for  $r_i$  to get:

$$r_i = \frac{\sqrt{f_i} \cdot N \cdot \alpha}{\sum_{j=1}^T \sqrt{f_j}} \tag{11}$$

The constraints are satisfied if  $\frac{1}{N \cdot \alpha} \leq \frac{\sqrt{f_i}}{\sum_{j=1}^T \sqrt{f_j}} \leq \frac{1}{\alpha}$  which proves part (i) of the theorem.

Without this condition on  $f_i$ , the above optimization can be re-written as the following Lagrangian taking all the constraints into account as:

$$G = \sum_{i=1}^T \frac{f_i \cdot C}{r_i} + \gamma_0 \left[ \sum_{i=1}^T r_i - N \cdot \alpha \right] - \sum_{i=1}^T \gamma_i \cdot (r_i - N \cdot \alpha) - \sum_{i=1}^T \beta_i \cdot (-r_i + 1)$$

The Kuhn Tucker Conditions for the modified Lagrangian are:

$$-f_i \cdot \frac{C}{r_i^2} + \gamma_0 - \gamma_i + \beta_i = 0; \forall i = 1 \text{ to } T \tag{12}$$

$$\sum_{i=1}^T r_i \leq N \cdot \alpha, \gamma_0 \geq 0, \text{ and } \gamma_0 \left[ \sum_{i=1}^T r_i - N \cdot \alpha \right] = 0 \tag{13}$$

$$r_i \leq N, \gamma_i \geq 0, \text{ and } \gamma_i \cdot (r_i - N) = 0; \forall i = 1 \text{ to } T \tag{14}$$

$$-r_i \leq -1, \beta_i \geq 0, \text{ and } \beta_i \cdot (-r_i + 1) = 0; \forall i = 1 \text{ to } T \tag{15}$$

Solving Eq. 12, we get,

$$r_i = \sqrt{\frac{f_i \cdot C}{\gamma_0 - \gamma_i + \beta_i}} \tag{16}$$

Equations 14 and 15 imply that either  $\gamma_i = 0$  or  $r_i = N$  and also either  $\beta_i = 0$  or  $r_i = 1$  respectively. Therefore, the optimum solution for  $r_i$  is given by,

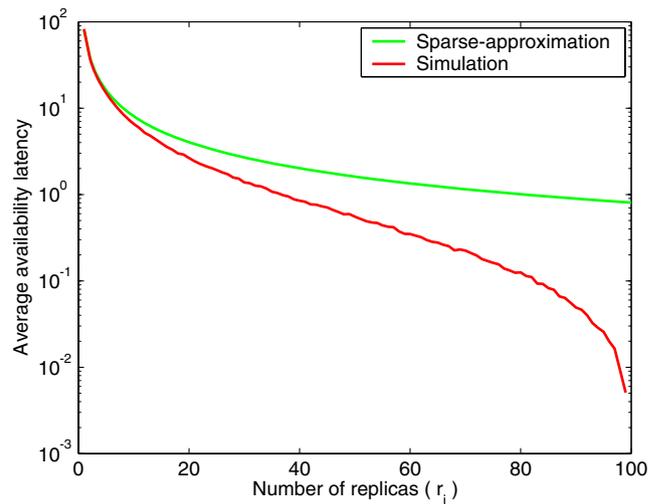
$$r_i = \max \left( 1, \min \left( \sqrt{\frac{f_i \cdot C}{\gamma_0}}, N \right) \right) \tag{17}$$

where  $\gamma_0$  is such that  $\sum_{i=1}^T r_i = N \cdot \alpha$  proving part (ii) of the theorem.  $\square$

Hence, in a sparse network, the optimal replication that minimizes the aggregate availability latency is obtained if the number of replicas for a data item is proportional to the square root of the frequency of access for that data item. Cohen and Shenker [5] proved that for unstructured peer-to-peer networks the expected search size is minimized using a square-root replication strategy which is shown to be optimal. The aggregate availability latency metric in wireless mobile ad-hoc networks is analogous to the expected search size used in peer-to-peer networks.

It should be noted that, in general, the optimal replication depends on how  $\delta_i$  is related to  $r_i$  i.e.  $\delta_i = F(r_i)$  and  $F(\cdot)$  is the function that will determine the optimal replication strategy. The above methodology can be used to be obtain the optimal number of replicas as long as  $F(\cdot)$  is differentiable.

Figure 2 shows the typical trend shown by  $\delta_i$  for a  $10 \times 10$  torus, where  $r_i$  is increased from 1 to  $N$  where  $N = 100$ . In other words, in a  $G = 100$  cell torus,  $N = 100$  cars are deployed, with  $r_i$  of them having a replica



**Figure 2** Sparse analysis (Eq. 6) versus simulation obtained average availability latency for a data item as a function of its replicas for a  $10 \times 10$  torus, when the number of cars is set to 100

for the data item. We only consider a single data item, a request for that item can be issued at any vehicle chosen uniformly at random among all the cars. If the item is stored locally, the latency is 0. This result is independent of the storage per car because a maximum of one copy of a given data item may be stored in a car. Figure 2 indicates that when  $r_i$  is small, ( $r_i \leq 20$ ) the analytical approximation in Eq. 6 is valid. Subsequently, latency reduces at a much faster rate when compared to that predicted by the sparse approximation. This is because for a given  $G$ , as  $r_i$  increases, the latency till any one of the  $r_i$  replicas is encountered can no longer be modeled as the minimum of  $r_i$  independent exponentials. In the next section, we provide an approximation that captures the high density case.

#### 4.1.2 Dense scenario

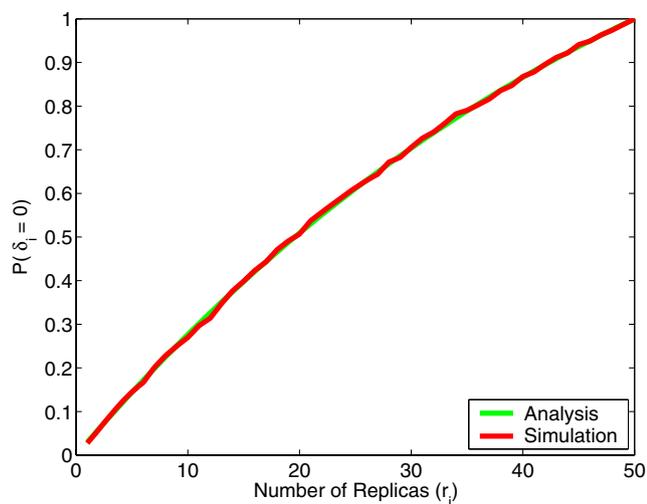
In this section, we provide an analytical formulation that captures the trends shown by the availability latency in the presence of a high density of replicas. Recall that  $N$  cars are distributed uniformly at random across  $G$  cells,  $r_i$  of the  $N$  cars carry a copy of the data item of interest. Here, we use the traditional definition of the expected availability latency for data item  $i$ ,  $\bar{\delta}_i = \sum_{k=0}^{\infty} k \cdot P(\delta_i = k)$ .

We first determine an expression for the case when the latency is 0. This occurs if the data item is locally stored at a client or a data item replica is located in the same cell as the client at which the request is issued.

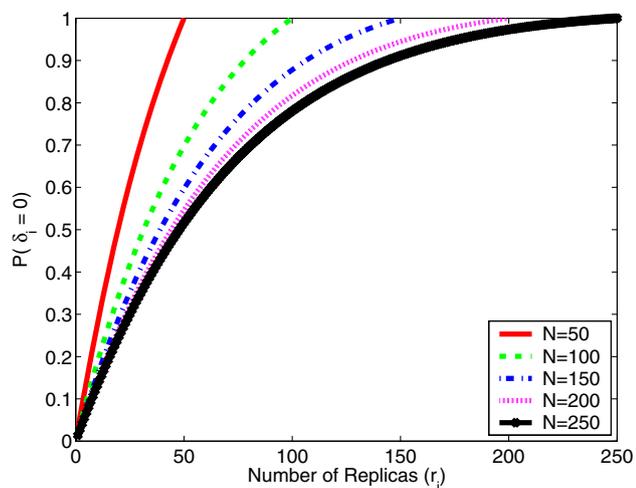
Hence, the probability that the latency experienced by a client is zero is given by the following expression:

$$P(\delta_i = 0) = \frac{r_i}{N} + \left(1 - \frac{r_i}{N}\right) \cdot \left(1 - \left(1 - \frac{1}{G}\right)^{r_i}\right) \quad (18)$$

Figure 3a indicates that the analytical expression above matches the simulation results quite well. For a given car density  $N$ , as the density of replicas increases, the probability that the availability latency experienced by a client is zero also increases. Figure 3b shows how this probability varies with increasing car density. Given a torus comprising  $G$  cells, increase in  $P(\delta_i = 0)$  shows a decreasing steepness as  $N$  increases. This is



(a)



(b)

**Figure 3** **a** shows the validation of the analytical expression in Eq. 18 for the probability that availability latency is zero when  $N = 50$ . **b** shows the probability that the availability latency is zero as a function of the replicas for the data item for 5 different car densities {50, 100, 150, 200, 250}

because with increasing  $N$ , the number of potential clients from which a request can be issued also goes up. Hence, a given value of  $r_i$  implies a greater percentage of the vehicles store the requested item  $i$  locally for a smaller  $N$  as compared to a larger one. Consequently, the corresponding  $P(\delta_i = 0)$  is lower for a smaller  $N$  as compared to a larger one.

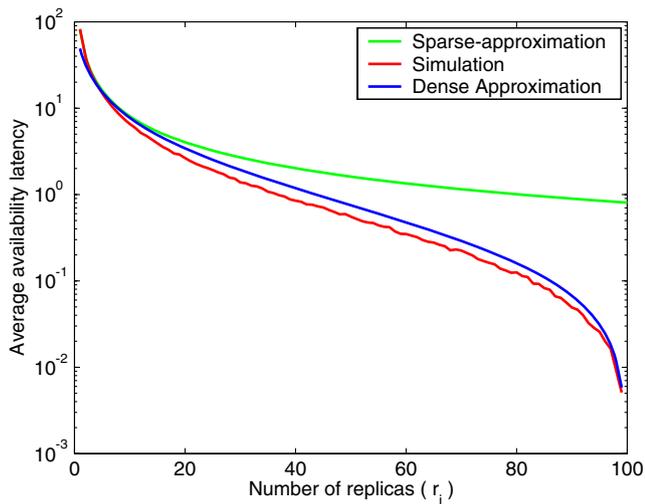
We provide an approximation assuming a memory-less mobility model without regards to the shape of the region across which the vehicles are moving. Define,  $A_k$ , the event that a data item  $i$  is encountered by the client for the *first* time in the  $k^{th}$  cell. This implies that the item  $i$  was not encountered in any of the previous  $k - 1$  cells. Let  $P(A_k)$  denote the probability of event  $A_k$  occurring. Note  $P(A_k)$  is a joint probability function. Let  $p_k$  denote the probability of encountering data item  $i$  in the  $k^{th}$  cell, given that it was not encountered in the previous  $k - 1$  cells. Note that  $p_k$  is a conditional probability. Also,  $p_1 = P(\delta_i = 0)$  as defined by Eq. 18. Then,

$$p_k = 1 - \left(1 - \frac{1}{G - k + 1}\right)^{r_i} ; 2 \leq k \leq G \quad (19)$$

Note that the model assumes that not encountering the data item in the  $(k - 1)^{th}$  cell increases the probability of encountering it in the  $k^{th}$  cell. Moreover, when  $k = G$ ,  $p_k = 1$  no matter what the value of  $r_i$ , meaning that the maximum latency that a client will encounter will always be  $\leq G$ . Although this is true for a high density of replicas, this approximation is not valid for a sparse replica density where  $p_k$  may not increase as  $k$  increases especially for the first few steps of the client.

Recall,  $P(A_k)$  is a joint probability since encountering a data item for first time in the  $k^{th}$  cell indicates that it was not encountered in any of the previous  $k - 1$  cells. Clearly,  $p_k$  and  $p_{k-1}$  are conditional probabilities that are not independent, hence, we use the following generalized multiplication rule to obtain the value of  $P(A_k)$  as,  $P(E_n \dots E_1) = P(E_n | E_{n-1} \dots E_1) \dots P(E_2 | E_1) P(E_1)$ .

This gives  $P(A_k) = p_k \prod_{j=1}^{k-1} (1 - p_j) ; 2 \leq k \leq G$ . Then, the average availability latency  $(\bar{\delta}_i)$  for data item  $i$  is given by,  $\bar{\delta}_i = \sum_{k=1}^G (k - 1) P(A_k)$ . Using this formulation, we plot Fig. 4 which captures the trend depicted by the average availability latency against replica densities where the sparse and dense approximations are plotted together with the latency obtained via simulations. However, when this approximation is plugged into the optimization represented by Eq. 3, the resulting numerical solution does not lend itself directly to determining the optimal replication exponent  $n$ . Hence, we employ simulations to obtain the optimal



**Figure 4** The complete picture depicting the availability latency for a data item obtained via simulations as compared with its sparse and dense approximation as a function of its replicas for a  $10 \times 10$  torus, when the number of cars is set to 100

replication exponent that minimizes the aggregate availability latency.

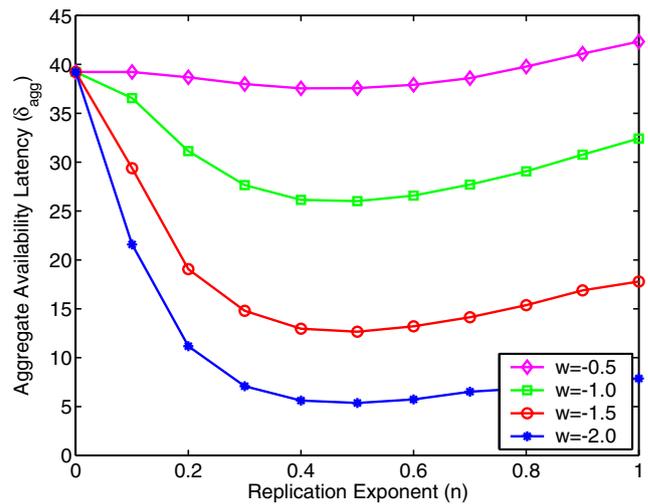
4.2 Simulation results of data items with display time = one

We present simulation results indicating the replication exponent range that provides near optimal aggregate availability latency. We also show how this latency is affected by the different parameters in the optimization space. In all our experiments, we assume that the various data item popularities are distributed as per the Zipf’s law [28]. This means that the frequency of the  $r^{th}$  popular data item is inversely proportional to its rank i.e.

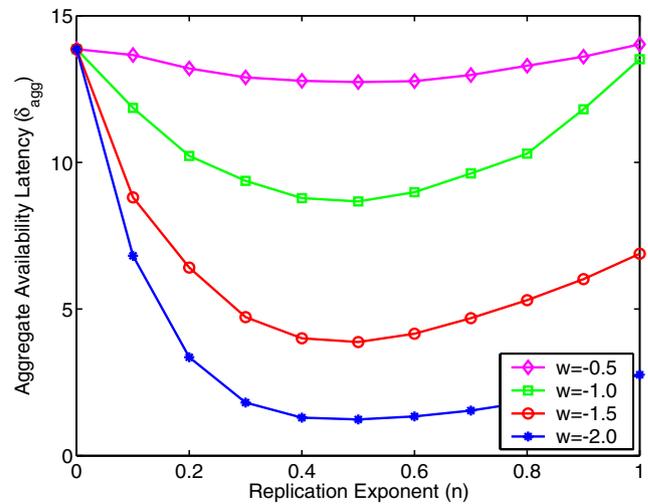
$$f_i = \frac{1}{\sum_{j=1}^T \frac{1}{j^v}}; 1 \leq i \leq T \tag{20}$$

Here, the exponent  $v$  controls the skewness in the popularity distribution of the data items. We denote  $w = -v$  as the skewness parameter. A higher absolute value of  $w$  indicates that most of the popularity weight is spread across the first few popular titles. Note that the data item repository size is  $T$  and the denominator is simply a normalization constant.

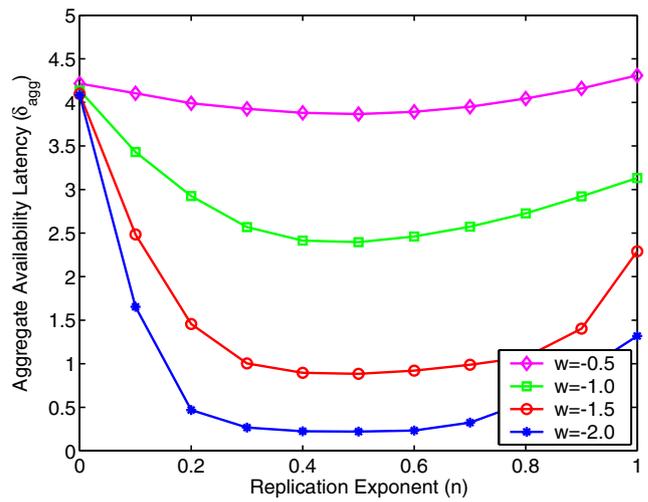
Figure 5 depicts the latency performance for different replication schemes when storage per car is increased from 4 to 25 slots. The title repository size is  $T = 100$  and the car density is  $N = 50$  which implies that the total storage  $S_T$  is increased from 200 to 1250 slots. As expected the latency decreases as storage



(a)  $\alpha = 4$



(b)  $\alpha = 10$



(c)  $\alpha = 25$

**Figure 5** Aggregate availability latency for different replication strategies for a  $10 \times 10$  torus when  $T = 100$  and  $N = 50$ . Figures a, b, and c depict three different storage values per car: {4,10,25}

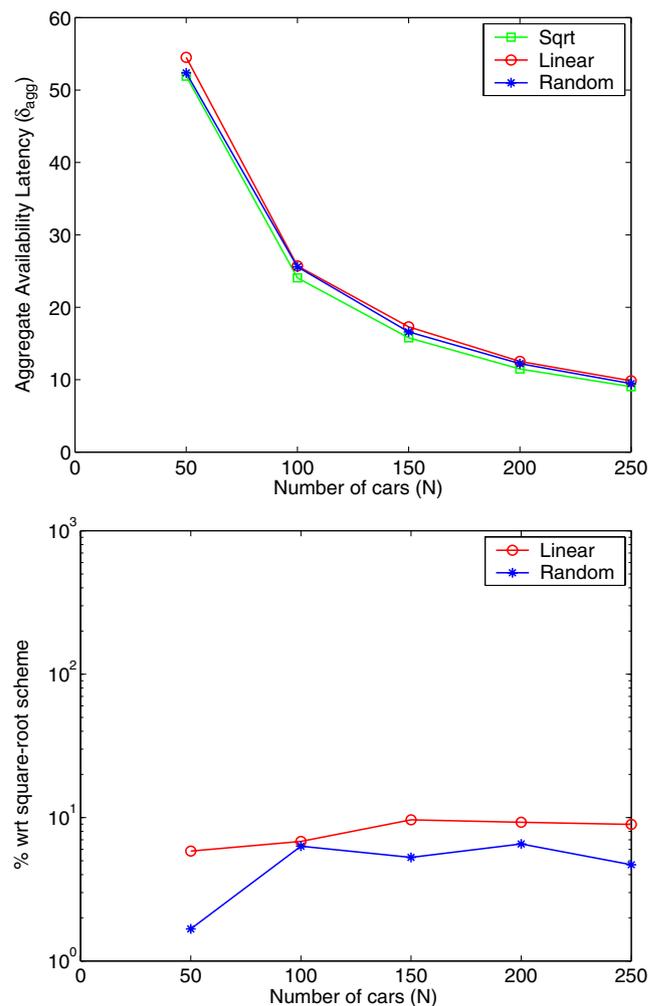
is increased. The replication schemes with exponent values 0, 0.5, and 1 have been popularly studied in the literature and are labelled random, square-root, and linear respectively. The value of  $w$  captures the skewness in the data item popularities, a higher value of  $w$  indicates that most of the popularity weight is spread across the first few popular titles. Below we describe the main observations from this figure.

The random scheme allocates the same number of replicas per data item irrespective of their popularity. Hence, in all cases, it yields the same aggregate availability latency irrespective of the value of  $w$ . As the replication exponent increases from 0 to 1 progressively more replicas are allocated for the popular data items. This increase in the replicas is accelerated for higher values of  $w$  that provide a bias for the popular titles. Hence, we see a sharp decrease in the availability latency from  $n = 0$  to  $n = 0.3$  for  $w = -1.5$  and  $w = -2$ . However, the maximum number of replicas per data item can never exceed  $N$ . For a value of  $w = -0.5$  in which case the popularity weight is spread more evenly among all the data items, it almost doesn't matter what the replication scheme is as seen by the relatively flat latency curves.

When storage per car is low,  $\alpha = 4$ , this represents a scenario with a sparse density of data item replicas. In this case, the square-root replication scheme provides the minimum latency. Also, the range where the replication exponent  $n$  varies from 0.4 to 0.6 shows a latency very close to the square-root scheme. This is true even when the data item popularities are skewed. Moreover, the range  $0.4 \leq n \leq 0.6$  shows near optimal latency performance even when the storage is increased (see Fig. 5b and c). In other words, through the entire spectrum of the replica density, a replication scheme defined by an exponent in this range will provide near optimal performance. For the rest of this study, we will consider the square-root ( $n = 0.5$ ) scheme as representative of this range and compare its performance to the two extremes namely, random ( $n = 0$ ) and linear ( $n = 1$ ). Next, we present results from a set of experiments that are representative of the general trend observed with respect to the relative performance of the three replication schemes.

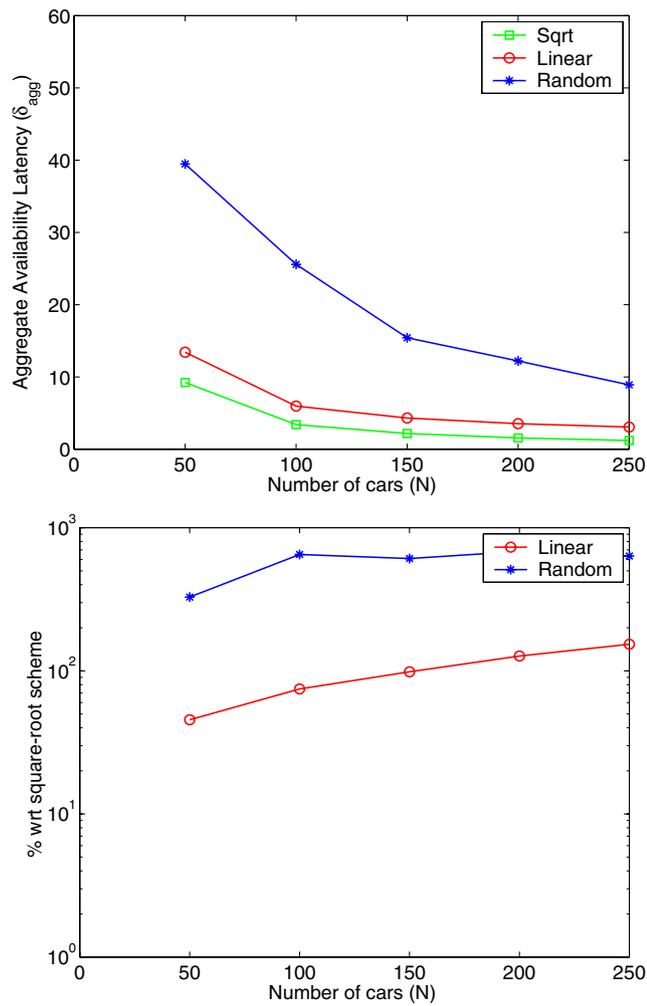
#### 4.3 Variation in car density

Figures 6 and 7 presents the performance of the three replication schemes, for popularity skewness values of  $-0.5$  and  $-2.0$  respectively, as a function of the car density when the storage per car is held constant at 3 for  $T = 100$ . Increase in the car density increases the total storage in the system. Hence, more replicas per data



**Figure 6** Aggregate availability latency for the three replication schemes as a function of the car density for  $w = -0.5$  when the storage per car is fixed at 3,  $T = 100$

item can be allocated resulting in an overall decrease in the aggregate availability latency. This is true for all replication schemes. However, here for  $w = -0.5$  and  $w = -1$  (beyond  $N = 100$ ), the random scheme shows slightly better performance than the linear scheme. This is because for low skewness parameters assigning equal number of replicas per data item is better than providing higher replicas for the popular data items which do not have a sufficiently high popularity weight. However, for higher skewness in popularity ( $w = -1.5$  and  $w = -2.0$ ), the behavior of the linear scheme starts paying richer dividends in reducing the overall latency, hence, it outperforms the linear scheme. In all cases, the square-root scheme always yields the lowest aggregate availability latency. Similar performance trends are observed when the storage in the system is varied by increasing the storage per car or increasing the data item



**Figure 7** Aggregate availability latency for the three replication schemes as a function of the car density for  $w = -2.0$  when the storage per car is fixed at 3,  $T = 100$

repository size keeping the other parameters constant. To avoid redundancy, we do not present those results here.

### 5 Data items with small size and short client trip duration

The analysis and simulation results presented so far assumed that once a request is issued at a client, it is willing to wait as long as it takes for its request to be satisfied. In other words, the client trip duration was assumed to be unbounded. For the specific mobility model under consideration, namely 2D random walk on a torus, the maximum latency experienced by a client is bounded [1] as long as at least one replica of every item is present in the system at all times. However, in more practical scenarios, the client may have a cer-

tain maximum time it is willing to wait for request resolution. This is captured by considering a finite trip duration,  $\gamma$ , for the client. The availability latency for item  $i$ ,  $\delta_i$ , can be any value between 0 and  $\gamma - 1$ . If the client’s request is not satisfied, we set  $\delta_i = \gamma$  indicating that the client’s request for item  $i$  was not satisfied.

### 5.1 Analysis

As before with Section 4.1, here, we derive expressions for average availability latency of a data item as a function of its replicas for a short client trip duration. Below, we present approximations in the case of low and high density of replicas.

#### 5.1.1 Sparse approximation

Recall that latency in the case of a 2D-random walk on a torus can be modeled as an exponential distribution as:

$$P(\delta_i > t) = \lambda \exp(-\lambda t) \tag{21}$$

where  $\lambda = \frac{r_i}{c \cdot G \cdot \log G}$ . The average availability latency with finite trip duration  $\gamma$  is then given by,

$$\bar{\delta}_i = \int_0^\gamma x \lambda \exp(-\lambda t) dx + \int_\gamma^\infty \gamma \lambda \exp(-\lambda t) dx \tag{22}$$

Hence, we get

$$\bar{\delta}_i = \frac{c \cdot G \cdot \log G}{r_i} \cdot \left[ 1 - \exp\left(\frac{-\gamma \cdot r_i}{c \cdot G \cdot \log G}\right) \right] \tag{23}$$

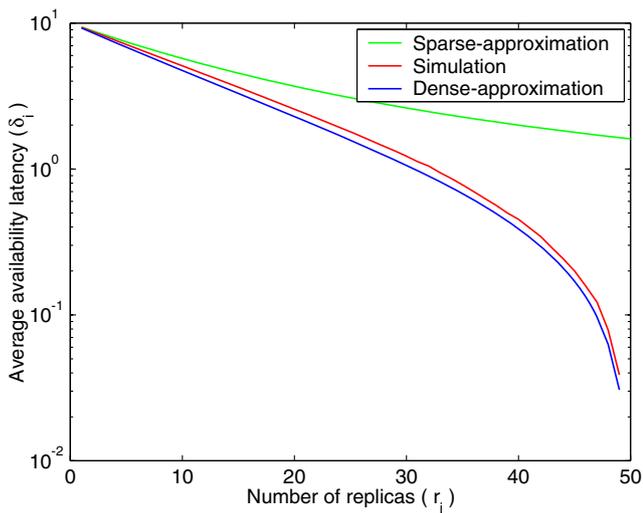
#### 5.1.2 Dense approximation

Recall that as defined in Section 4.1.2,  $A_k$  is the event that a data item  $i$  is encountered by the client for the first time in the  $k^{th}$  cell and  $P(A_k)$  is the probability that event  $A_k$  occurs. Also,  $p_k$  is the probability of encountering data item  $i$  in the  $k^{th}$  cell, given that it was not encountered in the previous  $k - 1$  cells. Then,

$$p_k = 1 - \left(1 - \frac{1}{G - k + 1}\right)^{r_i}; 2 \leq k \leq \gamma \tag{24}$$

Also, we rewrite  $P(A_k)$  incorporating the finite trip duration constraint as,  $P(A_k) = p_k \prod_{j=1}^{k-1} (1 - p_j); 2 \leq k \leq \gamma$ . Let  $P(A_{\gamma+1})$  denote the probability of not encountering the data item  $i$  during the entire trip duration  $\gamma$ . Hence,  $P(A_{\gamma+1}) = \prod_{j=1}^\gamma (1 - p_j)$  Then, the average availability latency for data item  $i$  is given by,  $\bar{\delta}_i = \sum_{k=1}^{\gamma+1} (k - 1) P(A_k)$ .

Figure 8 shows that the above approximations for low and high density of replicas matches the latency

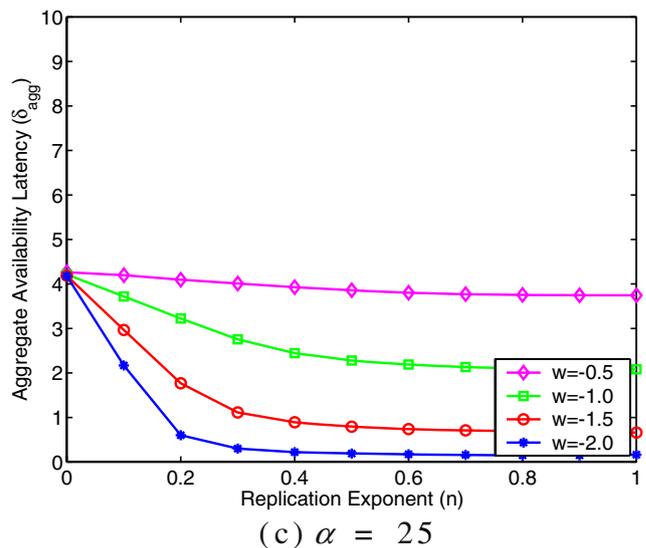
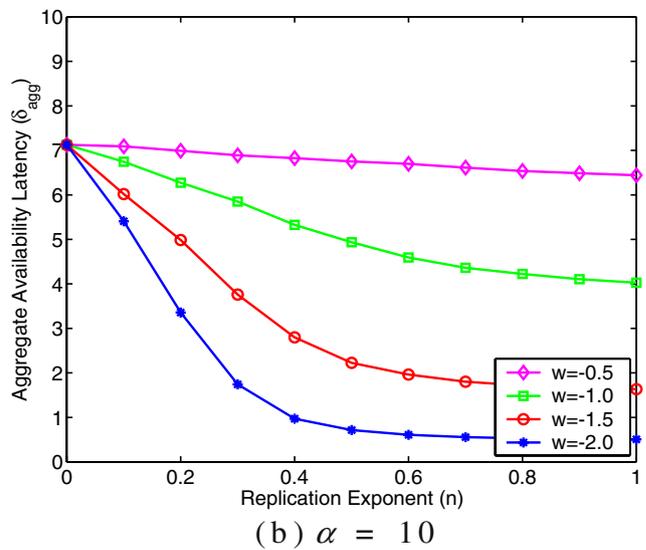
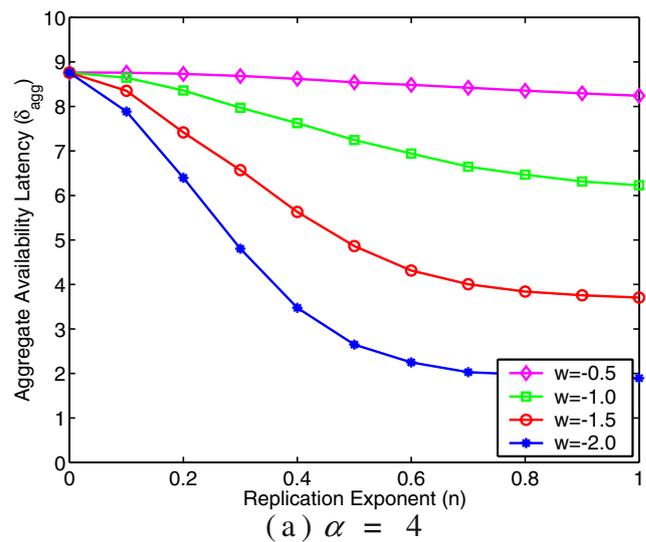


**Figure 8** Average availability latency for a data item as a function of its replicas for a finite trip duration  $\gamma$  of 10. The simulation curves are plotted along with the sparse and dense approximations for finite trip duration for a  $10 \times 10$  torus, when the number of cars is set to 50

obtained by simulations. In this case, the dense approximation is also valid for a low density of replicas because the finite trip duration  $\gamma$  limits the maximum value of the availability latency. For a low density of replicas in most cases the latency will be higher than  $\gamma$  and hence it will be bounded by  $\gamma$ . For a higher replica density, the value of  $\gamma$  is not as significant since the latency for that item will be much lower than  $\gamma$ .

5.2 Simulation results

Figure 9 depicts the latency performance for different replication schemes when storage per car is increased from 4 to 25 slots when the trip duration is set as 10. When storage per car is low,  $\alpha = 4$ , this represents a constrained storage scenario. The linear scheme that allocates more replicas to the popular data items shows superior performance as compared to the square-root scheme. This is because in such scenarios the replicas per data item is small, hence, only data items having a larger number of replicas will provide a latency less than  $\gamma$ . Since the popular data items are the ones that requested more often allocating more replicas for these items lowers the aggregate availability latency. Contrast this scenario with the case of unbounded trip



**Figure 9** Aggregate availability latency for different replication strategies for a  $10 \times 10$  torus for a finite trip duration of 10 when  $T = 100$  and  $N = 50$ . Figures **a**, **b**, and **c** depict three different storage values per car: {4,10,25}

duration where a square-root replication scheme always provided the minimum latency (see Fig. 5).

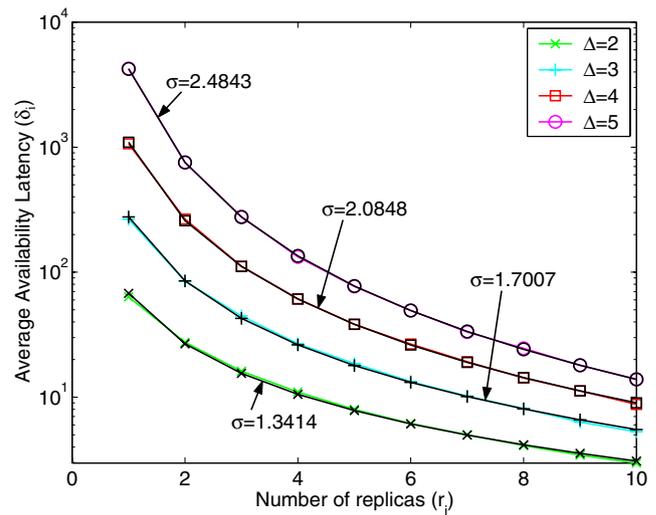
The optimal scheme here is a super-linear one which allocates most of the replicas to the first few popular items after satisfying the constraint that at least one copy of every item must be present in the network. For a highly skewed scenario,  $w = -2$ , allocating all the remaining storage for the most popular item minimizes the latency. This is because most of the popularity weight is associated with the most popular item which is requested very often.

As the storage per car is increased further the curves start becoming flatter and at  $\alpha = 25$ , see Fig. 9c, a replication scheme characterized by an exponent in the range,  $0.3 \leq n \leq 1.0$ , shows near optimal performance. This is because the storage is abundant enough for all these schemes to allocate a copy of the popular data items to every car bringing the latency for these items to 0. The difference in the replicas allocated for the lesser popular data items has minimal effect on the aggregate availability latency on account of their lower request rate. Recall, the frequency of access to the data items follows a zipf distribution that depicts a heavy-tailed behavior.

### 6 Data items with large size and long client trip duration

All the results presented so far considered a homogeneous repository of data items with a display time ( $\Delta$ ) of one. In this section, we consider data items with a higher  $\Delta$ . In such cases, the latency encountered by a client’s request is given by the earliest time when a contiguous block of  $\Delta$  cells containing at least one replica of the requested item is encountered. Here, we consider scenarios with long client trip durations and present a curve-fit based approximation that captures the relation between the average availability latency and the number of data item replicas. Hence, we present the optimal replication exponent that minimizes aggregate availability latency in the case of large data items and long client trip durations.

Figure 10 depicts the average availability latency for a data item with a higher display time ( $\Delta = \{2, 3, 4, 5\}$ ) as a function of the replicas for that item. For a given data item replica density, the latency increases with the display time. As expected the latency reduces with increase in the replicas. A simple curve-fit on the latency curves for all the  $\Delta$  values yields a close-match with the expression of the form  $\bar{\delta}_i = \frac{C}{r_i^\sigma}$  where  $\sigma$  represents the exponent for a given data item display time and



**Figure 10** Average availability latency for a data item as a function of its replicas for different data item display times for a  $10 \times 10$  torus. The latency is given by  $\frac{C}{r_i^\sigma}$  where the exponent  $\sigma$  increases with data item display time

$C$  is a constant that is a function of the size of the torus. Note that the value of  $\sigma$  for data items with a display time of one is one (see Eq. 6). The values of  $\sigma$  increase with data item display time. This indicates that an increase in the replicas provides a larger drop in the latency for a data item with a higher display time. Intuitively, encountering a replica in a contiguous block of  $\Delta$  cells becomes more and more difficult as  $\Delta$  increases. Hence, an increase in the replica density provides a faster reduction in the latency for the higher  $\Delta$  items. This is captured by the increasing value of  $\sigma$  with  $\Delta$ .

The specific formulation  $\bar{\delta}_i = \frac{C}{r_i^\sigma}$  has special significance since it can be plugged in directly into the optimization formulation in Section 4.1.1 to determine the optimum replication scheme that minimizes the availability latency in case of data items with higher display times.

*Remark* In case of a sparse density of vehicles, with a repository of data items with higher display times ( $\Delta > 1$ ), the replication exponent  $n$  that minimizes the aggregate availability latency is such that  $n < 0.5$ .

Following a similar procedure as the proof listed in Theorem 1, we obtain the optimal replication exponents for the  $\sigma$  values capturing higher data item display times in Fig. 10. Table 2 lists the display times and the corresponding approximate optimal exponent values.

**Table 2** Approximate optimal replication exponents for data items with higher data item display times

$\Delta$	$\sigma$	$n = \frac{1}{\sigma+1}$
2	1.3414	0.4271
3	1.7007	0.3703
4	2.0848	0.3242
5	2.4843	0.287

## 7 Data items with large size and short client trip duration

In this section, we consider scenarios with short client trip durations with data items having higher display times. This implies that the client is only willing to wait for a short period for its request to be satisfied (denoted by  $\gamma$ ). Otherwise the request is tagged with a latency equal to  $\gamma$ .

As with the previous simulations, we assume that the cars employ a 2D random walk based mobility model. Here, we set the client trip duration,  $\gamma$ , as 6,  $N = 200$ , and  $T = 100$ . We simulated a skewed distribution of access to the  $T$  data items using a zipf distribution with a mean of 0.27. The distribution is shown to correspond to sale of movie theater tickets in the United States [6].

Initially, all cars are distributed across the cells of the map as per the steady state distribution which is determined by a random number generator initialized with a seed. Depending on the particular replication technique, the replicas for each data item are calculated using Eq. 2 and then distributed across the car. A car only contains a maximum of one replica for a particular data item. The allocation of data item replicas across the cars is uniform. At each step, depending on the current car location, it moves to one of its adjoining cell (including itself) as governed by the mobility model. Another seed determines the choice of which cell a car moves to. Since  $\gamma = 6$ , each car performs six transitions according to the mobility model. We performed the comparisons for several different data item distribution seeds starting from the same initial car positions. Next, we varied the initial car positions by changing the initial seed. Specifically, we chose 50 different initial seeds and for each of these we used 50 seeds that decide the distribution of the data item replicas among the cars. Thus, each point in all the presented results is an average of 2500 simulations.

Below is an overview of the key lessons learned from these experiments with higher data item display times and a short trip duration.

(a) The optimal value of  $n$  varies as a function of the scarcity of the network storage (b) When storage is scarce, the optimal aggregate availability latency is

realized by using a higher value of  $n$ . (c) Even a random scheme with  $n = 0$  is good enough when storage is abundant relative to the repository size.

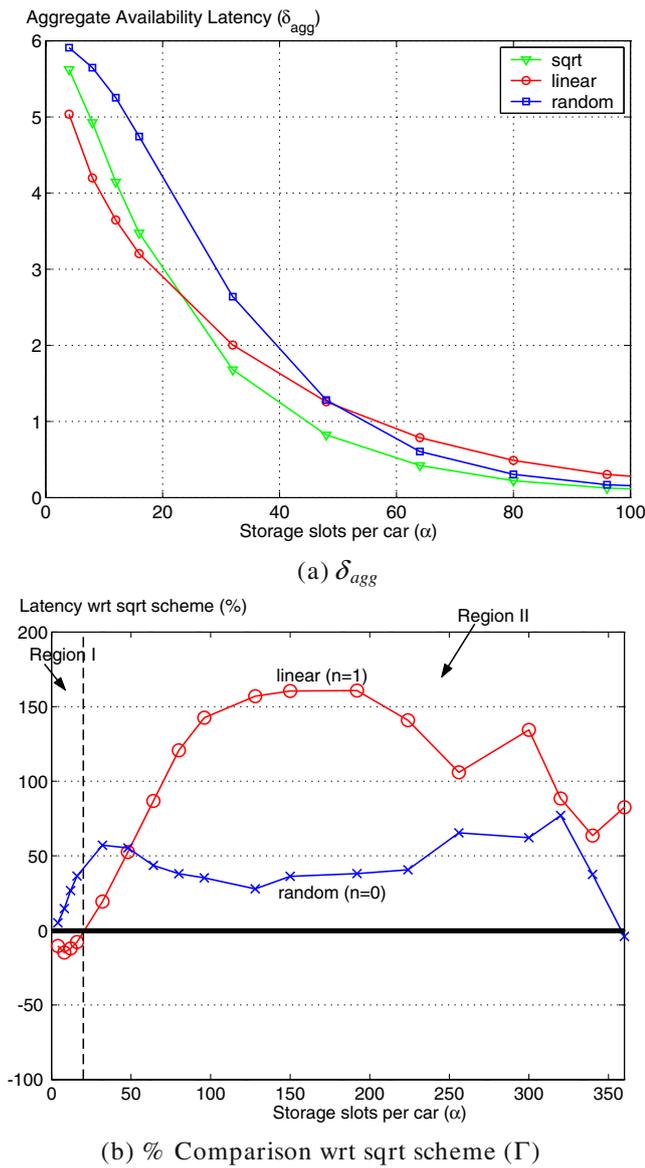
When storage is extremely scarce, with larger data item sizes ( $\Delta > 1$ ), linear ( $n = 1$ ) scheme provides the best performance. This is because it allocates more replicas for the popular data items at the cost of assigning very few for the remaining data items. In this case, the contribution to  $\delta_{agg}$  is a function of the  $\delta$  for the more popular data items since for the less popular data items there will be insufficient replicas to reduce their  $\delta$ . On the other hand, since the random scheme is blind to the data item access frequencies, on an average, it assigns equal number of replicas for each data item thereby providing the worst performance.

The square root ( $n = 0.5$ ) scheme assigns fewer replicas for the popular data items than the linear scheme. As we increase the amount of storage, there is a cut-off point along the storage axis, where allocating more replicas for the popular data items provides negligible improvement in  $\delta_{agg}$ . It is beyond this point that the square root scheme starts outperforming the linear scheme. This is because the square root scheme can use the extra storage savings for allocating replicas for the less popular data items thereby reducing their  $\delta$ .

To illustrate, Fig. 11 shows the variation of  $\delta_{agg}$  as a function of  $\alpha$  for  $\Delta = 4$ . Since  $\delta_{agg}$  is a function of the value of  $n$ , hence, here we denote it as  $\delta_{agg}(n = i)$ . For Fig. 11b, the y-axis represents the percentage comparison of the linear ( $n = 1$ ) and the random ( $n = 0$ ) schemes with respect to the square root ( $n = 0.5$ ) scheme calculated as,  $\Gamma = \left( \frac{\delta_{agg}(n=i) - \delta_{agg}(n=0.5)}{\delta_{agg}(n=0.5)} \right) \times 100$ ; where  $i = \{0, 1\}$ .

Figure 11b shows two distinct regions in which the schemes with  $n = 0.5$  and  $n = 1$  perform well under certain parameter settings within the design space. For  $\alpha \leq 20$ , the linear scheme ( $n = 1$ ) performs the best. For  $20 \leq \alpha \leq 360$ , the square root scheme ( $n = 0.5$ ) performs the best. Beyond this value, even a random scheme ( $n = 0$ ) provides a competitive latency performance.

With  $\Delta = x$  and  $T = y$ , the value of  $\alpha$  needed to replicate the entire database on each car is  $\alpha_{db} = x \cdot y$ . At a certain storage threshold (earlier than  $\alpha_{db}$ ), the random scheme assigns enough replicas to the popular data items to bring their  $\delta$  down. In this case, all the data items have the same number of replicas, thereby producing a low  $\delta$  for every data item. Hence, from this point onward, even a random scheme provides adequate performance. However, this point requires sufficient storage per car and hence a random scheme may be appropriate only for over-provisioned scenarios. As



**Figure 11** **a** shows  $\delta_{agg}$  of the sqrt, linear and random replication schemes versus  $\alpha$  for  $\Delta = 4$  and  $N = 200$ . **b** shows the percent comparison of the linear and random schemes wrt the sqrt scheme for this scenario. Region I and Region II, respectively, indicate the parameter space where  $n = 1$  and  $n = 0.5$  perform the best

illustrated in Fig. 11b with  $N = 200$ ,  $T = 100$ , and  $\Delta = 4$ , the storage threshold is around 360 slots per car. For  $\Delta = 5$ , and 6, this threshold is approximately 450 and 540, respectively. These are loose upper bounds.

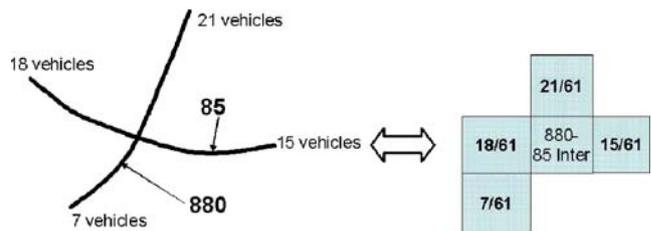
### 8 Evaluation with a map of San Francisco

In this section, we describe the performance of the various replication schemes when the vehicular move-

ments are dictated by an underlying map of the San Francisco Bay Area depicting major freeways and their intersections. We superimpose a 2D-grid on this map and the individual cells are labelled with the respective freeway id that they cover. This 2D-grid serves to capture the underlying map at a coarse granularity. Most of the probability mass is concentrated on the cells that represent the major freeways. The non-labelled cells have equal transition probabilities to each of its neighboring eight cells.

The outgoing transition probabilities at a cell that represents an intersection between two freeways are calculated as follows. As an example, consider the intersection of the freeways 880 and 85 as shown in Fig. 12. We obtained the traffic density seen on the freeways before and after the intersection from Caltrans data provided by the California department of transportation [24]. The website allowed real time gathering of vehicle traffic data. We considered a time window between 7–8 pm for a particular week and averaged the vehicular density seen during this period. The day-to-day statistics were quite similar, here, we show an example of how the actual data was converted into the probability transition values that formed the basis of the Markov mobility model. Similar calculations were employed to populate the entire transition probability matrix. Finally, we converted the  $15 \times 15$  grid into a torus by allowing cars at the boundaries to appear at the opposite ends with equal transition probabilities.

The transition matrix was used to generate the car movements. We provide a notion of directionality to the car movements by ensuring that the next step for a cars movement takes into account both the current cell as well as the previous cell which a car traversed. This is done by storing both the cell ids as part of the state of the Markov chain. Consequently, the flip-flop movements of the cars is avoided thereby ensuring that car movements are constrained by the underlying freeway structure of the map and are not entirely random. We

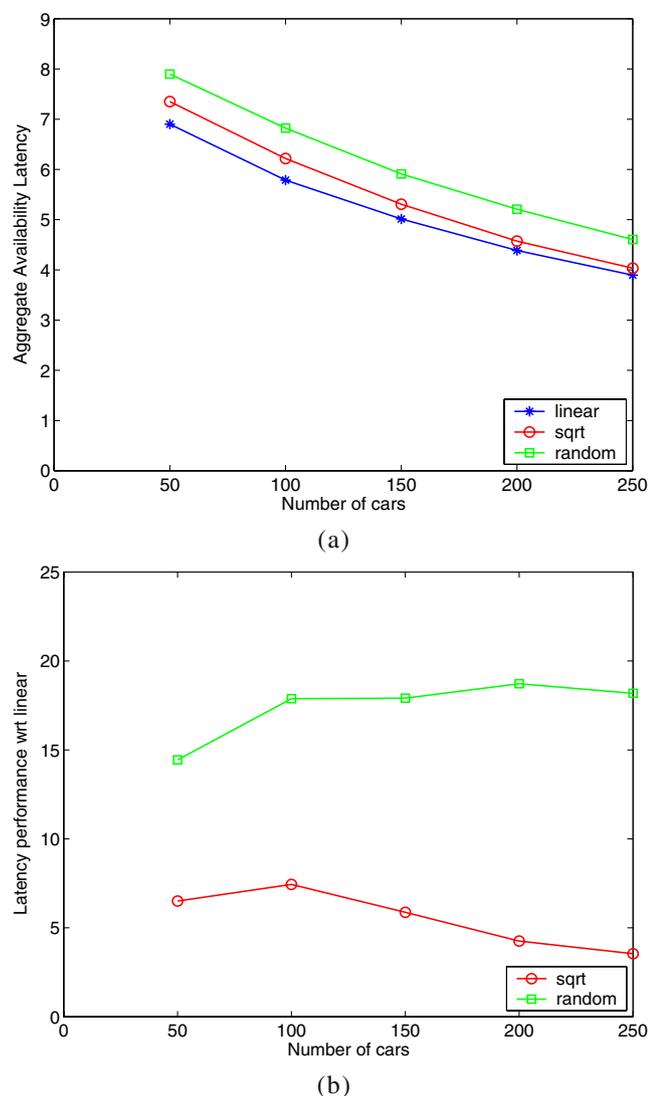


**Figure 12** The intersection between freeways 880 and 85 is captured in the figure along with the equivalent probability transitions in the Markov model based on data obtained from Caltrans regarding the vehicular densities

used these car movements to investigate the relative performance of the various replication schemes under such a scenario.

### 8.1 Results with replication schemes

In this section, we present some representative results for the various replication schemes obtained by employing the Markov mobility model previously derived from a map of the San Francisco Bay area. Employing aggregate availability latency as the chief performance metric for comparison between the linear, square-root, and random schemes; we explored the following parameter space: storage per car, data item repository size, and car density. As an example illustration, we present



**Figure 13** Performance of various replication schemes as a function of car density when  $T = 25$ ,  $\alpha = 2$ , and  $\gamma = 10$ . Figure **b** shows the performance wrt the linear scheme

performance results with variation in car density. As before, requests are issued, one at a time at each time-step at vehicles in a round-robin manner, as per a Zipf distribution with a mean of 0.27. For data item repository size  $T$  set as 25, client trip duration,  $\gamma$ , set as 10, storage per car,  $\alpha$ , set as 2, the latency performance with the various replication schemes is studied as a function of increasing car density  $N$  (see Fig. 13).

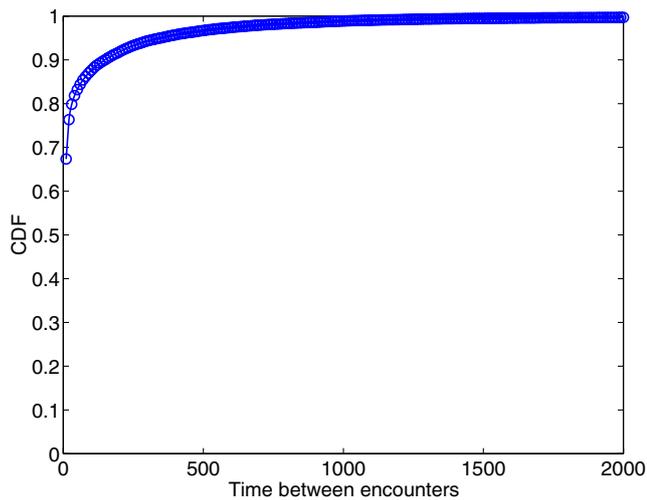
In all cases, the main conclusion is that the linear replication scheme shows superior performance as seen in Section 5 for the case with data item size = 1 and finite client trip duration. The trends seen with this model are similar to those seen with a uniform Markov mobility model with equal transition probabilities. This is because the map for the former causes some cells to be visited more than others, however, the movements of the vehicles still remain essentially Markovian. This result suggests that the uniform probability transition matrix based Markov model may be a good indicator of the performance that may be seen with a model derived from real maps.

## 9 Evaluation with real movement traces

In this section, we evaluate the latency performance of the static replication schemes using traces obtained from a bus-based DTN test-bed called UMassDieselNet [4]. First, we briefly describe the test-bed and present some properties of the mobility model followed by the buses. Then, we describe the details of the experimental set-up and the results comparing the square-root, linear, and random replication schemes under different parameter settings using these traces.

### 9.1 UMassDieselNet traces

In this section, we briefly describe the details of the UMassDieselNet test-bed and present some properties of the mobility model that characterizes the movement of the vehicles that are part of the test-bed. The UMassDieselNet network operates daily around the university campus and the surrounding county. It comprises of 30 buses equipped with a Linux based computer coupled with a IEEE 802.11b wireless interface that permits ad-hoc communication between the buses when they are in radio range. An IEEE 802.11b access point is also connected to the brick computer that allows DHCP access to passengers within the bus. The traces are available for a period of 60 days, the logs describe every encounter between every pair of buses that occurred during the day. The identity of the buses involved in the encounter, the time of encounter and amount of data



**Figure 14** The CDF of the time between encounters averaged across all the traces for the UMassDieselNet data set

transmitted during the encounter are logged in the trace files. Certain buses had long routes while others had short ones. Unfortunately, due to technical difficulties, the GPS device on the buses were unable to provide details about the bus locations.

The number of buses that were active on each day of the 60 day period during which the traces were collected varied from as low as 6 to as high as 24. We only consider traces where the number of active buses was greater than 15. This accounted for 52 traces. In general, the traces indicated a sparse density of buses with a high degree of locality in the encounters. In other words, if two buses encounter each other at the beginning then they will continue to encounter each other more frequently than other buses. This is captured in Fig. 14 where we plot the CDF of the time between consecutive encounters of the same pair of buses.

## 9.2 Experimental set-up

In this section, we describe the details of the simulation set-up used for evaluation of the replication schemes employing the UMassDieselNet traces. Each trace represents the movements of buses during that particular day. There is no correlation between trace movements across days. Hence, we process each trace at a time and then average the results observed across all the days noting that the average is indicative of the performance seen on most days. However, certain days do appear as outliers since the number of active buses differs from day-to-day.

As before, we consider a finite data item repository of size  $T$ . Each bus is assumed to carry  $\alpha$  storage slots. Replicas for each data item are determined based on a

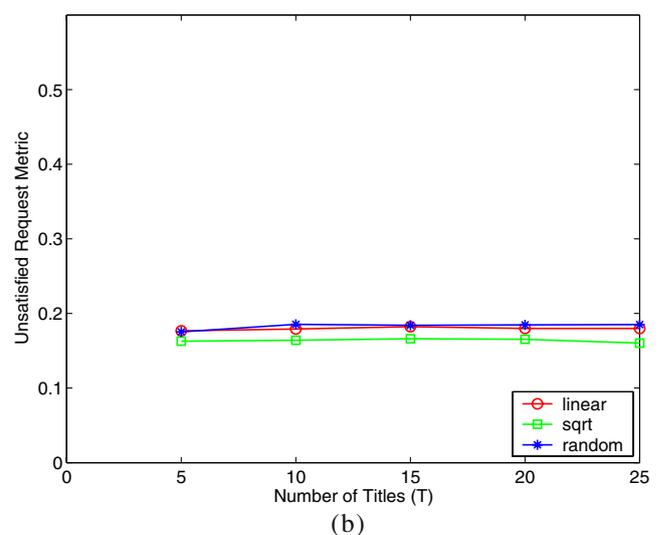
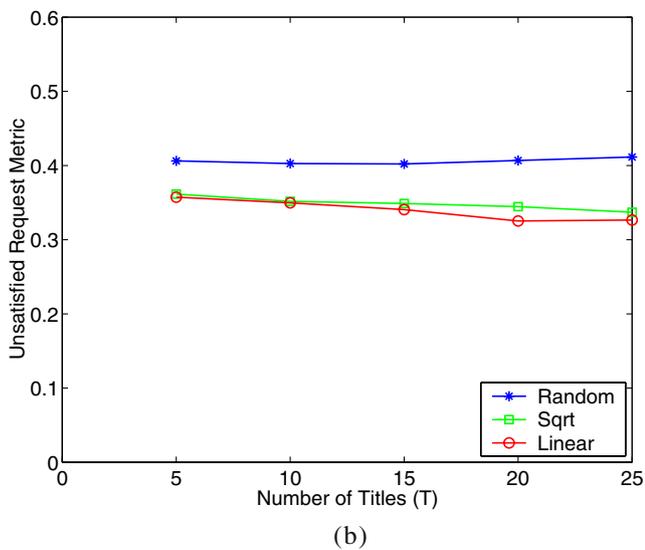
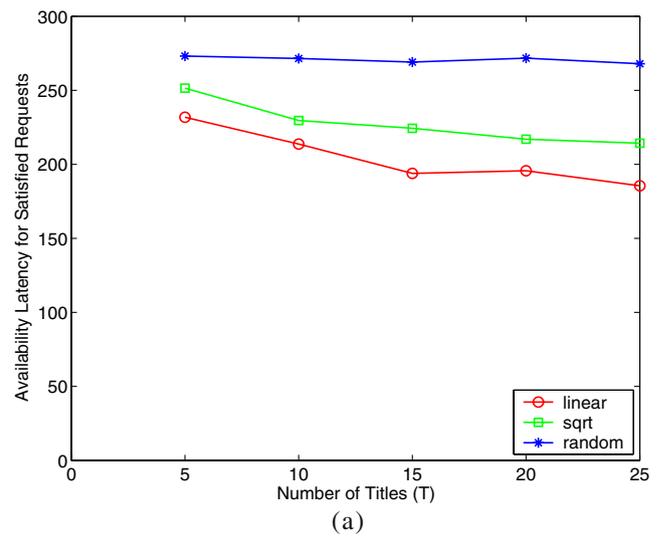
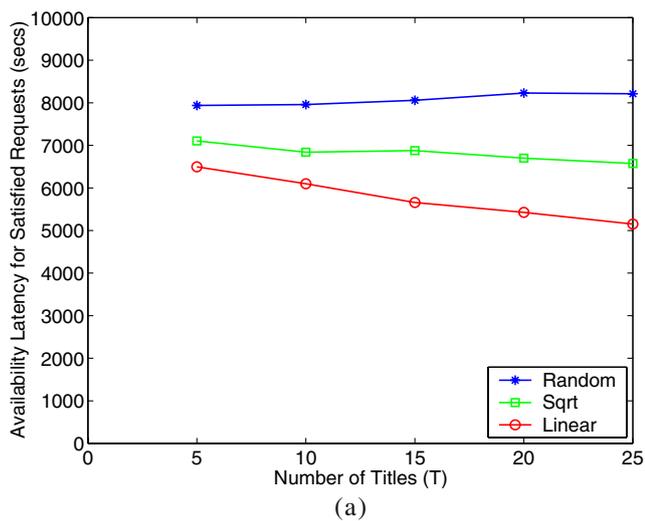
replication scheme and then allocated across the buses uniformly at random. The constraint is that at least one copy of every data item must be present in the network at all times. We consider the three representative replication schemes: random, square-root, and linear and study the relative performance of the schemes.

Since the buses only operate for a finite amount of time we consider two separate metrics (i) Average availability latency for satisfied requests (ii) Normalized unsatisfied request rate. Requests for the  $T$  titles are generated as per a Zipf distribution with an exponent  $w = -0.73$ . The duration during which the buses were active during a day is determined a priori and subject to this duration, requests are issued at equal inter-arrival times. A generated request is assigned to a bus chosen uniformly at random. A request is assumed to be satisfied either if the data item requested is locally stored or another bus carrying the requested item is encountered at some point after the request is issued. Those requests that are not satisfied at the end of the day are tagged as unsatisfied requests.

## 9.3 Results

We briefly describe the main results from evaluation of the performance of the replication schemes using the UMassDieselNet traces. For the first set of experiments, we vary the values of  $(T, \alpha)$  as  $\{(5,1), (10,2), (15,3), (20,4), (25,5)\}$ , see Fig. 15. The linear replication scheme provides the lowest average availability latency for satisfied requests (about 10–25% better than the square-root scheme). The linear and square-root scheme show similar performance in terms of the normalized unsatisfied requests. The random scheme shows poor performance both in terms of latency as well as the normalized unsatisfied requests.

Similar results are obtained when the storage per car is kept fixed and the size of the data item repository is increased. The mobility model provided by the traces represents an extremely sparse density of buses where inherently there is a limit to the maximum amount of time for request satisfaction (namely the last encounter time on the trace). The finite trip duration in conjunction with the low density and encounter model favors a linear scheme which allocates more replicas for the popular data items. The popular data items are requested more frequently and within the finite time for request satisfaction, have a higher probability of being satisfied on account of the larger number of replicas. The square-root scheme tries to allocate replicas less aggressively to the more popular data items in favor of the less popular ones. This hurts its performance since the less popular data items have a very low probability



**Figure 15** Aggregate availability latency for satisfied requests and the aggregate unsatisfied request metric for the random, square-root, and linear replication schemes are shown in **a** and **b** respectively. The ratio of the storage per car to the data item repository size,  $\frac{\alpha}{T}$  is maintained as 1:5

**Figure 16** Aggregate availability latency for satisfied requests and the aggregate unsatisfied request metric as obtained from an equivalent scenario employing the Markov model. The ratio of the storage per car to the data item repository size,  $\frac{\alpha}{T}$  is maintained as 1:5 (**a**, **b**)

of being satisfied. Notwithstanding, in such scenarios, a random scheme that allocates replicas equally across the data items shows the worst performance.

We now consider an equivalent scenario with the Markov mobility and study its properties in terms of the time between encounters. The aim is to capture a similar scenario as depicted by the UMassDieselNet traces (compare with Fig. 14). We consider a similar set-up to experimental scenario described in Fig. 15. Similar to the trends seen with the traces, Fig. 16 shows that the linear replication scheme outperforms the square-root and the random schemes in terms of the latency for satisfied requests. The performance in terms of the normalized unsatisfied requests is quite similar for the three schemes. These results suggest that the results

obtained from the Markov mobility model may be applicable across a vast range of scenarios comprising different mobility models. Adequate adjustment to the transition probabilities of the Markov model may enable this model to suitably capture the mobility trends of other models such as Manhattan, Highway, Random way-point etc.

### 10 Conclusions, discussion, and future research directions

In this study, we have systematically explored how data replication impacts the user latency to desired content

in a vehicular network. We presented an optimization formulation that minimizes availability latency across a repository of data items subject to storage constraints per vehicle. The solution to this optimization yields the optimal replication scheme, characterized by an exponent  $n$  that defines the number of replicas for a data item as a function of its popularity. Using mathematical analysis and simulations, we showed how the optimal replication exponent varied as a function of the three critical factors: data item size, the client trip duration, and the total storage in the system. While the evaluation above was based on the assumption of a random walk mobility model for the vehicles, we validated a subset of our observations employing two real data sets. The first was based on a city map with freeway traffic information while the second employed traces listing encounters between buses that were part of a small test-bed.

First, while our study indicates that replication has a significant impact on latency performance in an AutoMata-based application, we did not directly address how a replication scheme may be realized. This presents a fruitful future research direction. A promising approach is to employ a two-tier architecture [8] comprising of a low-bandwidth control plane between the base-station and vehicles, and a high-bandwidth data plane representing the ad-hoc, peer-to-peer network between vehicles. While all the data exchange takes place via the data plane, the control plane enables centralized information gathering at a suitable dispatcher. The dispatcher is aware of information such as the total number of cars, the available storage per car, the data item requests etc. On the basis of the target replication scheme to be realized, the dispatcher computes the total number of replicas to be maintained for each data item. Hence, every time a request is satisfied, depending on the current replicas of the requested item in the system, the dispatcher decides whether a client vehicle should create a new copy of that item. If such a process is followed, then after a cold-start phase where replicas are being created and deleted, the data item replica distribution will approximate the targeted one. Second, this study can be extended in terms of heterogeneity with respect to several parameters. The data item repository may have a mix of different sizes, the vehicles may have different amounts of available storage and different trip durations depending on their data item request preferences, and popularity distribution of the data items may change over time, especially when new items are introduced in the system. Each of these extensions adds another dimension in terms of practicality towards realizing such a system.

Third, we do not explicitly address contention and bandwidth issues within our model. Recently, Jindal and Psounis [21] have provided a contention model that can be easily incorporated in our study promising a richer evaluation.

Fourth, our study is based on static replication schemes, in that we do not explore any dynamic data re-organization schemes that reactively or pro-actively change the replica distribution depending on the requested items. In a related study, once static replication schemes have allocated replicas for the various data items, vehicles are employed as data carriers [9] to deliver data items from server vehicles carrying items to clients requesting them. The study shows that significant latency improvements can be obtained by employing these intermediate data carriers.

Finally, vehicular ad-hoc networks are an emerging area and many of the results presented here may be general enough to be applicable in a wide variety of contexts such as in intermittently connected mobile networks, mobile sensor networks, and other delay tolerant networks.

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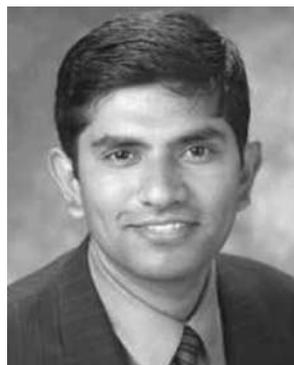
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