

4/29/12

## Class Lecture notes

## Congestion Control in Wireless Networks

- The need for Explicit Congestion Notification to deal with the problem of loss differentiation.

- The need for Congestion sharing to alleviate fairness problem arising due to shared medium.

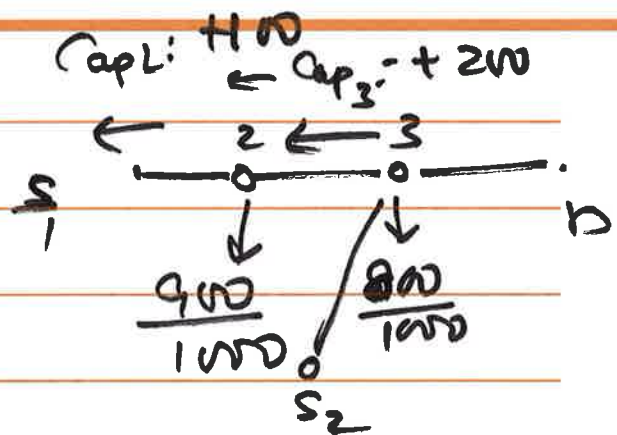
Both of these solutions require greater intelligence to be embedded at the core of the network, i.e. in the routers, violating the end to end architecture of traditional Internet.

Another new idea in congestion control is "explicit & precise rate control"

• contrast w/ AIMD approach

for general (i.e. wired) networks:

IRCP by Dukkipati & McKeown



Also a router-centric approach  
(hence not adopted earlier)

Big Industry development:

OpenFlow Routers —

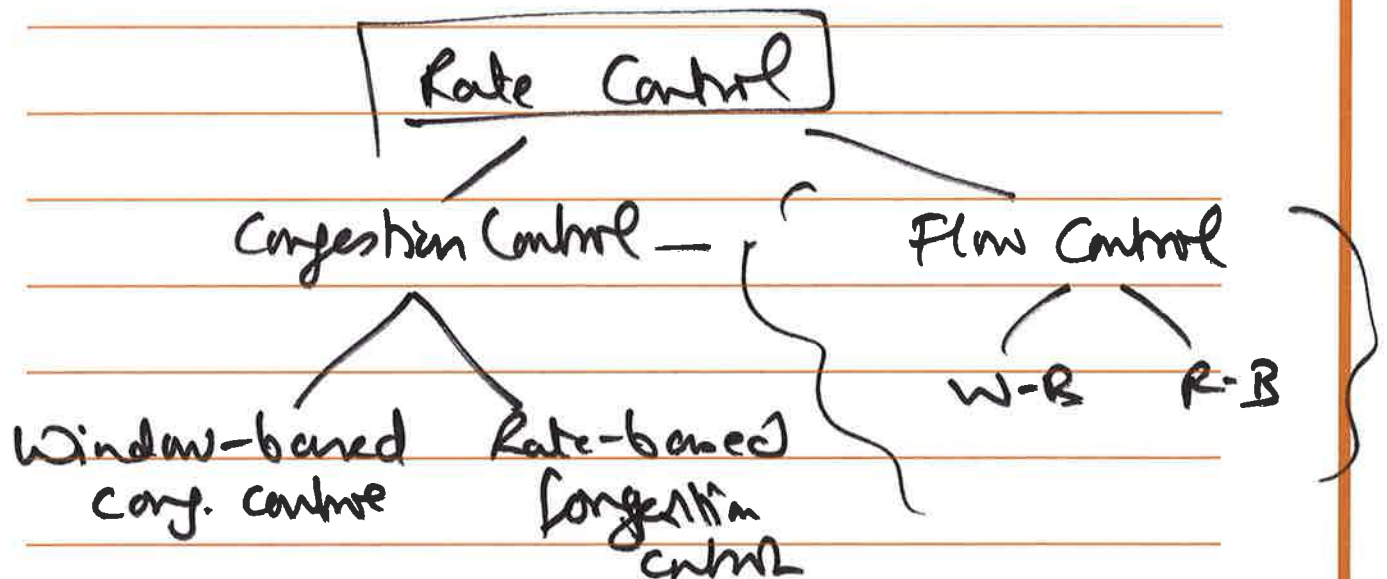
Software defined routers

This is likely to speed adoption of router-centric protocols for wired networks

Examples in Wireless networks of  
E&P rate control:

- WRCP for sensor networks
- WCP-Cap for Mesh networks

Congestion Control with Backpressure



Observation: Can solve some of the congestion-control problems such as fairness, at the MAC layer.

Recall max Backpressure Scheduling weight algorithm:  
schedule independent set of links that max  $\sum_{l \in I} w_{ij}^c$

where  $w_{ij}^c = (\phi_i^c - \phi_j^c) \cdot R_{ij}$

BCP was a distributed impl. at the routing layer (mostly)

DiffQ : an <sup>dist.</sup> implementation of Backpressure at the MAC layer



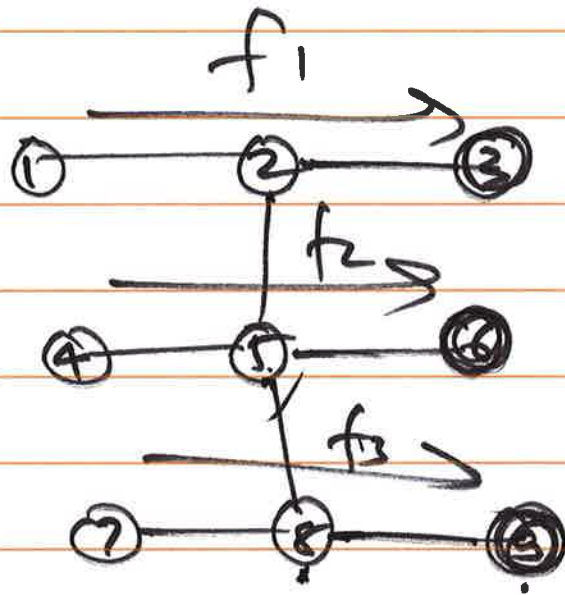
Basic idea of Diff Q:

choose the backoff interval based on  $\Delta Q_{ij}$  (i.e.  $w_{ij}$ ).

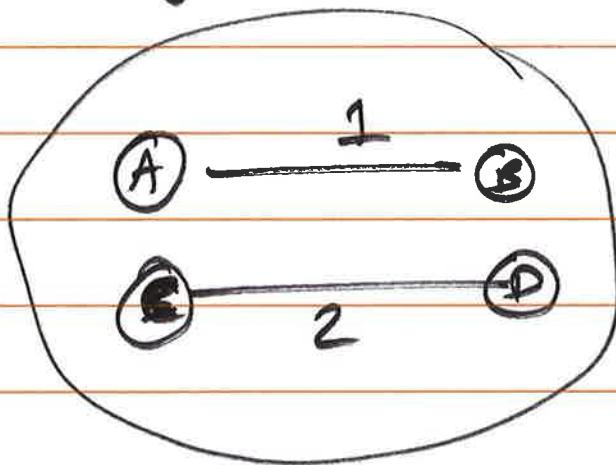
if we want to prefer transmissions on link w/ higher weight, want to make the ~~B~~ max Backoff window smaller.

Diff Q: look for 802.11e

which specifies different B.O. window sizes for different QoS classes, & map the  $w_{ij}$  to classes.

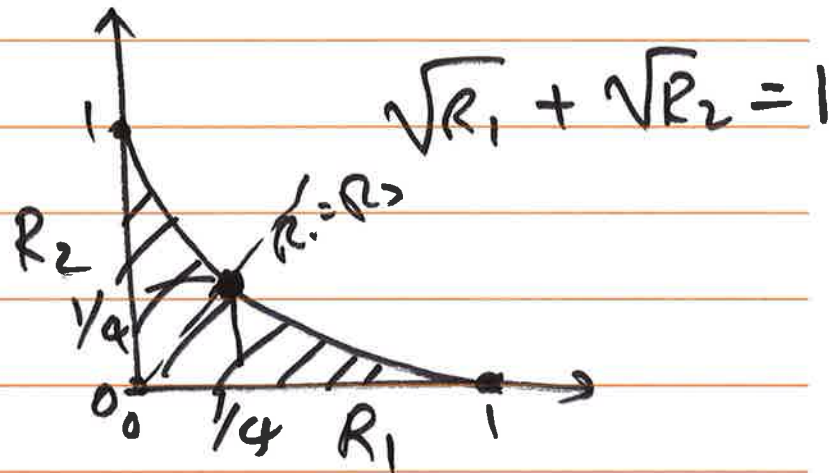


## Utility-based rate control



MAC layer:  
slotted  
Aloha.

Slotted Aloha Saturated Throughput  
Region:



Throughput efficient solution:  $(1, 0)$   
 $(0, 1)$

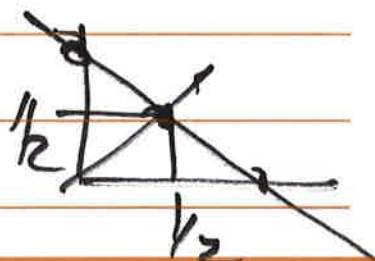
Sum rate = 1.

Clearly least fair solution!

Most Fair solution :  $(1/4, 1/4)$

least sum rate :  $1/2$ .

w/ TDMA, can get both.



Kelly '98

Utility-based rate allocation

$$\begin{aligned} \max \quad & \sum_i g_i(r_i) \\ \text{s.t.} \quad & \vec{r} \in \Delta \end{aligned}$$

rate region  
of the network.

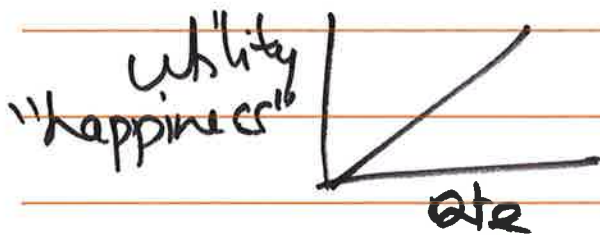
$i \leftarrow i^{\text{th}}$  flow.  
 $r_i \leftarrow$  rate  
allocated  
to flow  $i$

$g_i(\cdot)$  is a  
utility  
function.  
that is concave  
(second

derivative  
negative)  
or zero.)  
& nonnegative

Special cases of  $g_i(r_i)$ .

Linear utility :  $g_i(r_i) = c_i r_i$



Log utility :  $g_i(r_i) = c_i \log(1+r_i)$





w) slotted Aloha example

$$c_i = 1 \quad \forall i$$

Linear utility

$$\max R_1 + R_2$$

$$\text{s.t. } \sqrt{R_1} + \sqrt{R_2} \leq 1$$

$$\Leftrightarrow \max R_1 + R_2$$

$$\text{s.t. } \sqrt{R_1} + \sqrt{R_2} = 1$$

Solns: either  $R_1 = 1 \quad R_2 = 0$

OR  $R_2 = 1 \quad R_1 = 0.$

Log utility - proportional fair utility

$$\max \log R_1 + \log R_2$$

$$\text{s.t. } \sqrt{R_1} + \sqrt{R_2} = 1$$

$$\sqrt{R_2} = 1 - \sqrt{R_1}$$

$$R_2 = (1 - \sqrt{R_1})^2$$

$$\max \log R_1 + \log (1 - \sqrt{R_1})^2$$

↔

$$\max (\log R_1 + 2 \log (1 - \sqrt{R_1}))$$

$$\frac{\partial \cdot}{\partial R_1} = 0 \Rightarrow \frac{1}{R_1} + \frac{2 \cdot (-1)}{(1 - \sqrt{R_1}) \sqrt{R_1}} = 0$$

$$(1 - \sqrt{R_1})(\sqrt{R_1}) = R_1$$

$$\sqrt{R_1} - R_1 = R_1$$

$$\sqrt{R_1} = 2R_1$$

$$\sqrt{R_1} = \frac{1}{2}$$

$$R_1 = \frac{1}{4}$$

$$\Rightarrow R_2 = \frac{1}{4}$$

$$\text{Soln : } \left( \frac{1}{4}, \frac{1}{4} \right)$$

more  
Generally:  $\alpha$ -fair  $\Rightarrow$  utility  
function

---

Prof. Mike Neely's Dissertation  
at MIT:

utility optimization in a  
Backpressure framework

How to maximize utility  
C.i.e. pick a desired  
rate allocation across the  
flows / commodities while  
ensuring stable operation.

pb:  $\max \sum g_i(r_i)$

s.t.  $r_i \in \triangleleft$

↑  
Stability region  
of the network

Solution:

Part 1: rate allocation

Each source picks rate  $r_i$

to maximize: only needs local queue state!!!

$$(V \cdot g_i(r_i) - Q_i \cdot R_i)$$

Part 2: use max weight scheduling algorithm as before.



Part 1 rate control

$$V g'(R_i) - \Phi_i = 0.$$

pick  $R_i$  :  $g'(R_i) = \frac{\Phi_i}{V}$

$$\underline{R_i} = g'^{-1}\left(\frac{\Phi_i}{V}\right)$$

$V$  parameter trades off between utility optimization & average queue size (hence delay).

can be hard to find the best value of  $V$  for a given network sensitive to the topology & traffic